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Abstract

Road alignment is a process of high complexity, as from a set of inexhaustible solutions a unique solution is chosen which is a mixture of conflicting variables. In this thesis an attempt was made to automate vertical alignment of the road. For the research implementation, two stochastic methods were used: a heuristic, the Monte Carlo method and a metaheuristic, genetic algorithms, which are considered reliable for the optimization of vertical alignment in relation to other methods. The optimized grade line is produced minimizing the volume of earthworks while respecting the applicable national road rules. The user inputs road speed, road category, soil type and a list of geometrical data for the road. At the same time it is possible to enter the number of inflection points of the grade line. Otherwise, the program produces three solutions with different number of inflection points of the grade line between zero and a maximum number of inflection points which depends on the length of the road. The program was tested with real world data of roads which have already been studied/constructed all over Greece. The grade lines produced by the program approach optimally the terrain, thus respecting the demands of road design. The produced grade lines were also compared to the original grade lines of the available road studies, and the produced grade lines were found to be similar or better.

Keywords: Optimization of Vertical Alignment, Genetic Algorithms, Monte Carlo Algorithm, Optimization Methods

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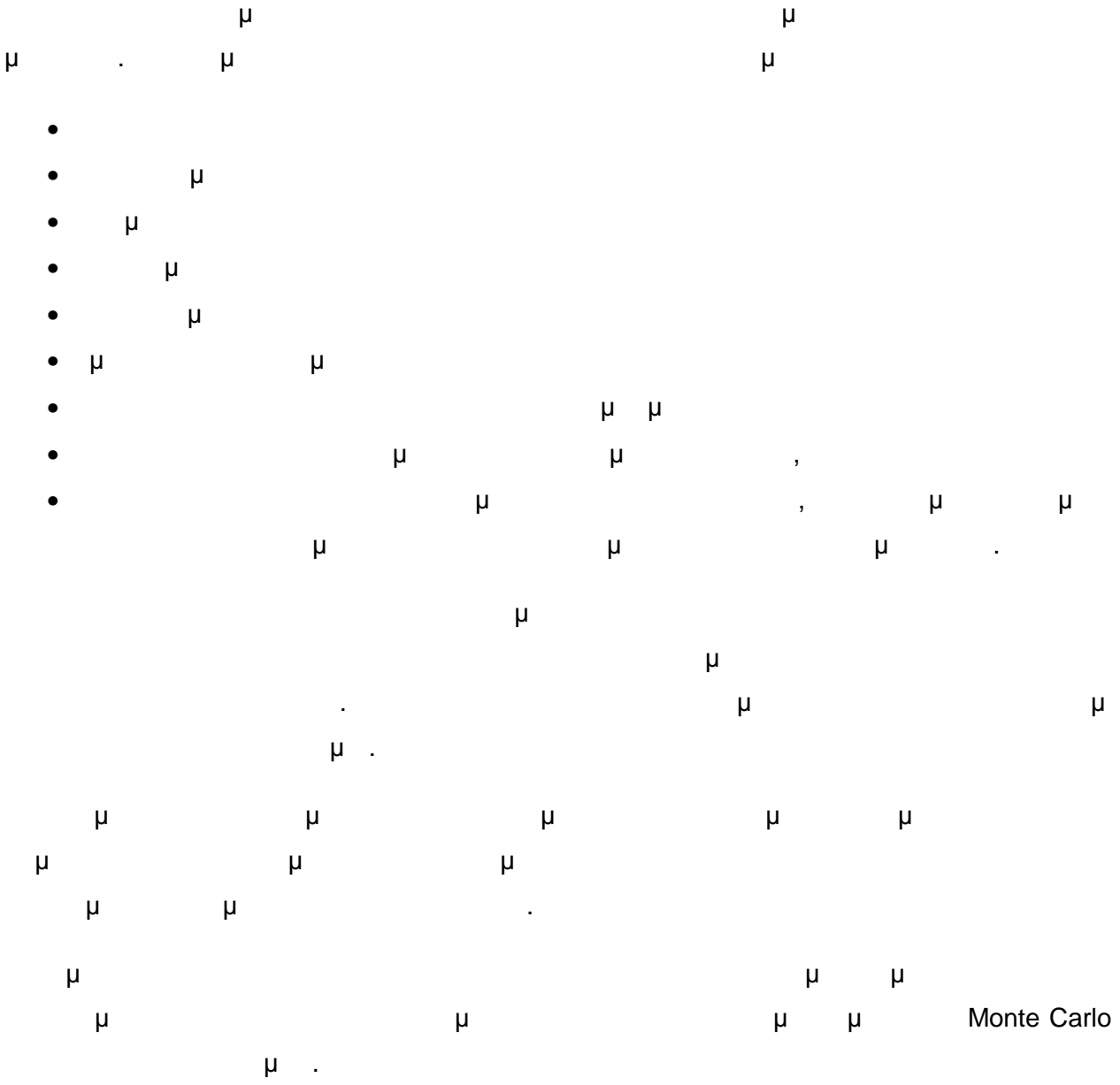
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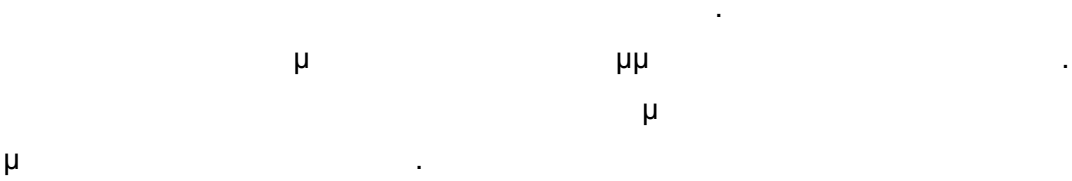
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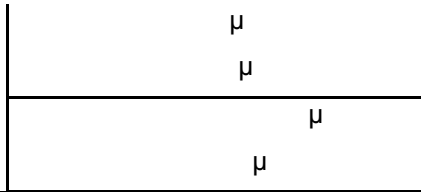
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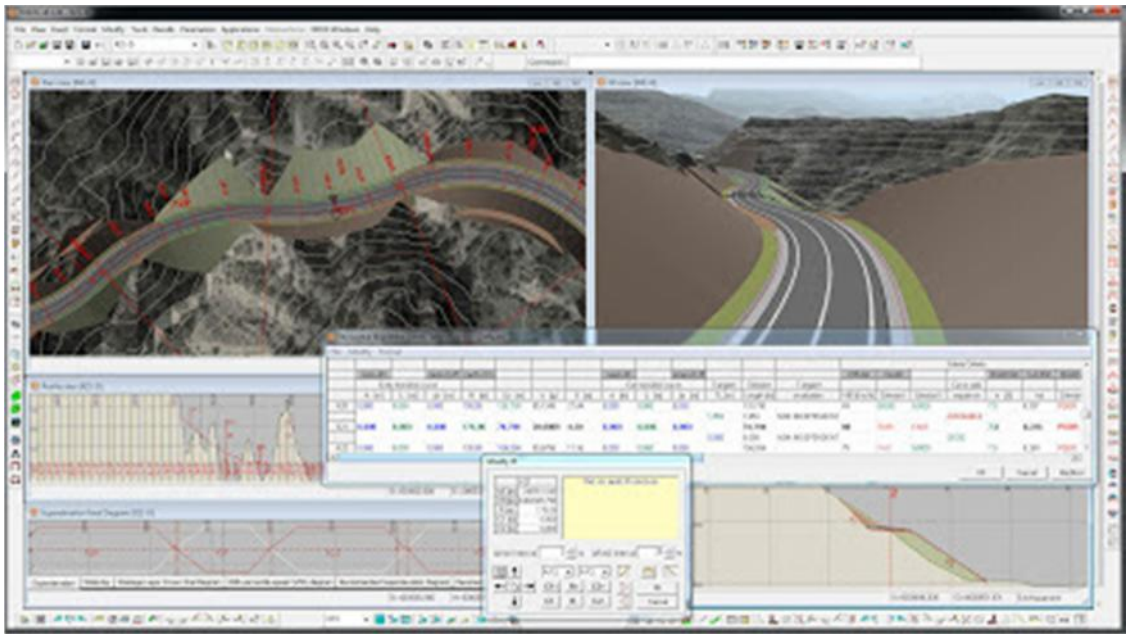
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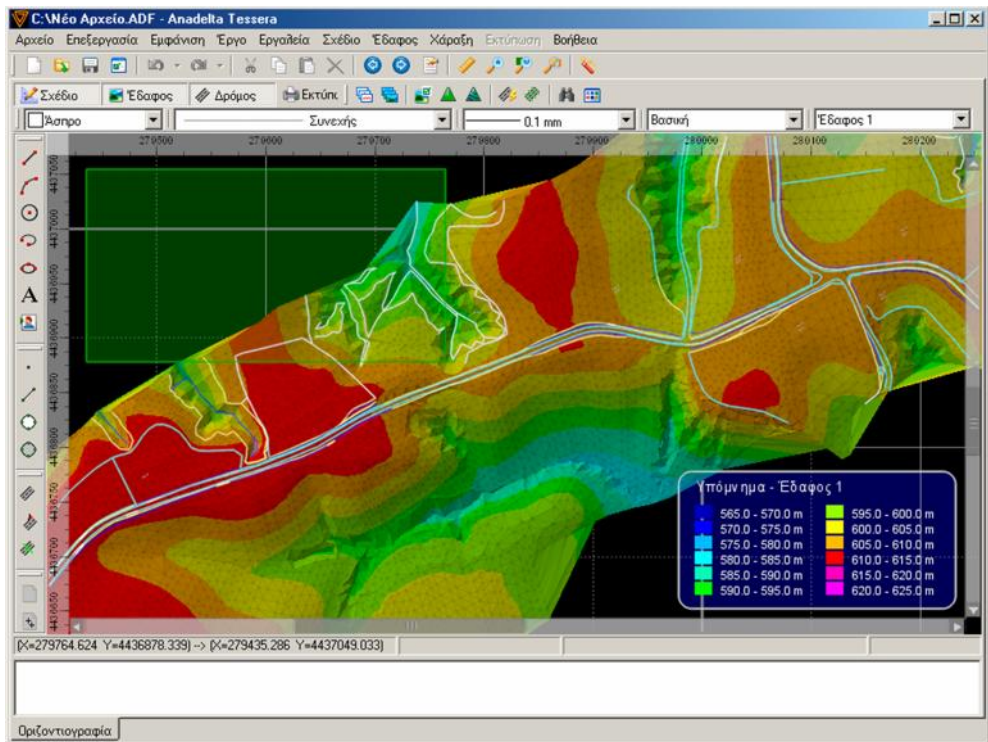
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Anadelta Software.

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 Undo/Redo, , μ , snap μ .. μ
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4: μ μ : anadelta.com

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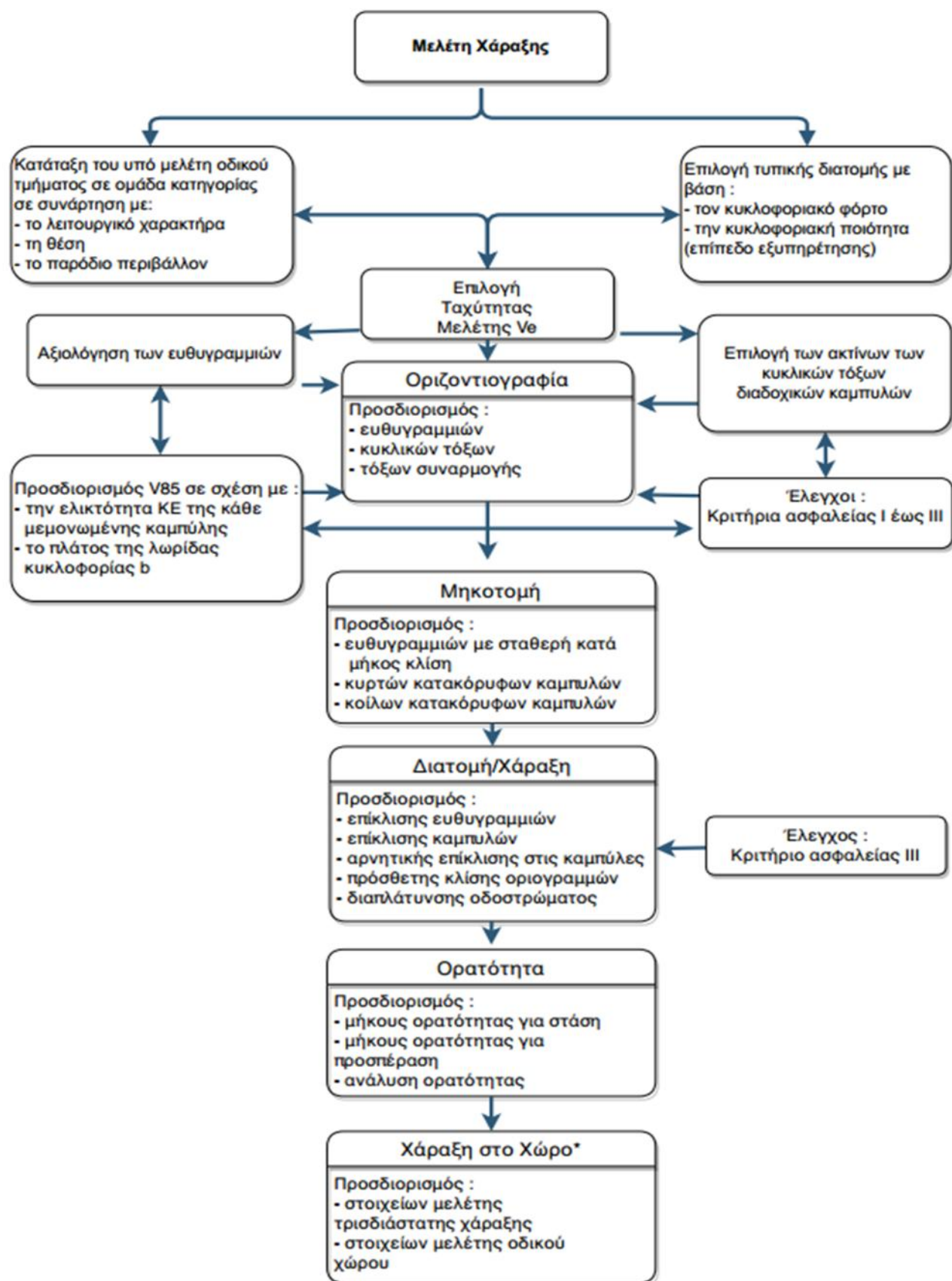
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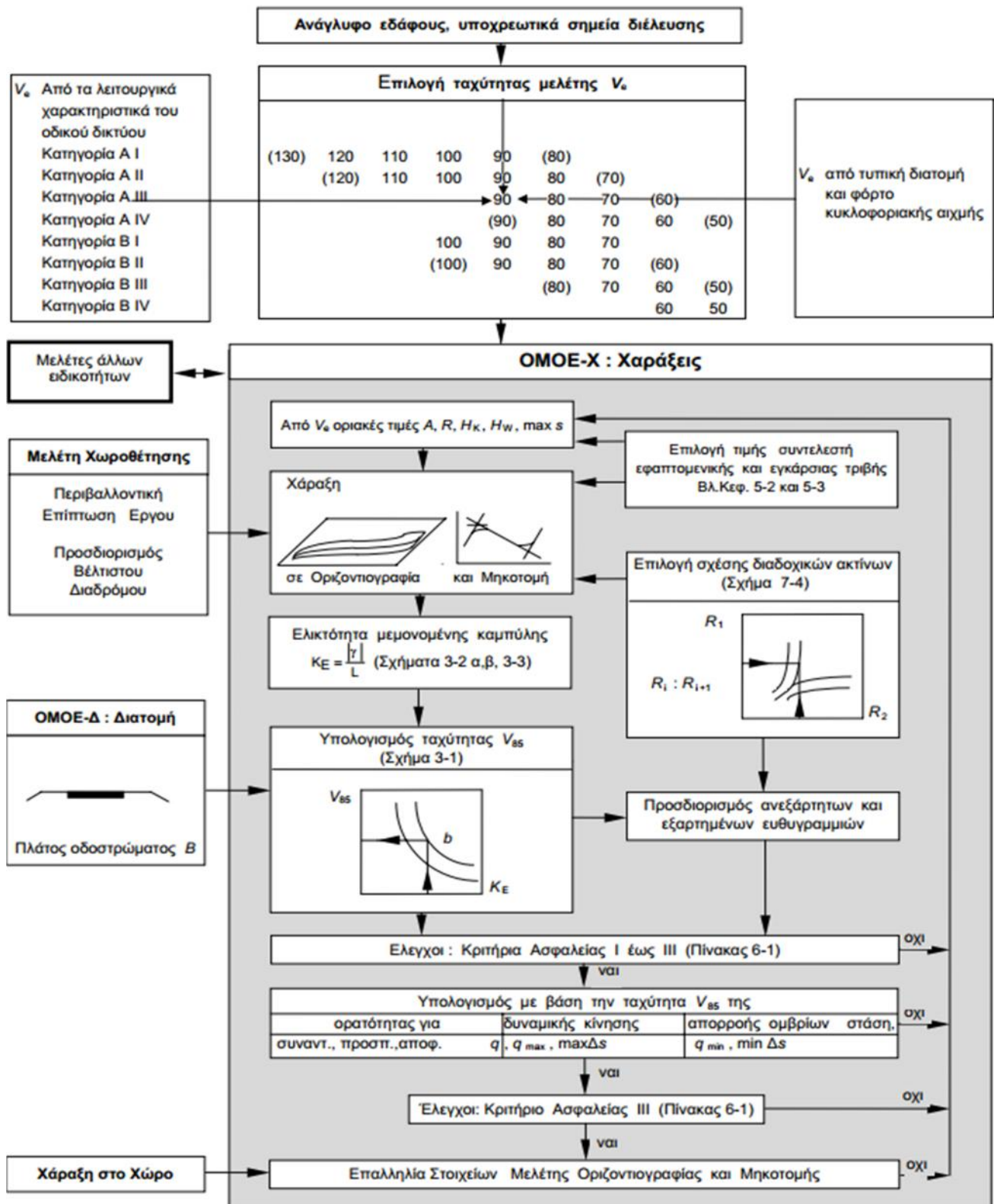
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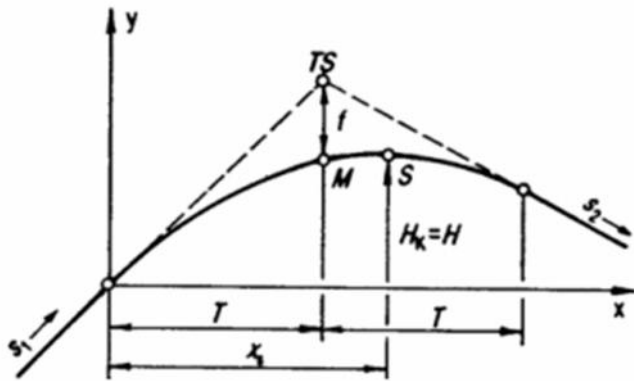
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(s = 0%).

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$$H_w = 0,5 \cdot H_k$$



$$x_s = -\frac{s_1}{100} \cdot H$$

$$s(x) = s_1 + \frac{x}{H} \cdot 100$$

$$y(x) = \frac{s_1}{100} \cdot x + \frac{x^2}{2 \cdot H}$$

$$T = \frac{H}{2} \cdot \frac{s_2 - s_1}{100}$$

$$f = \frac{T^2}{2 \cdot H} = \frac{T}{4} \cdot \frac{s_2 - s_1}{100} = \frac{H}{8} \cdot \left(\frac{s_2 - s_1}{100} \right)^2$$

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- μ : $T_{\min} = V_e$
- μ : $T_{\min} = 0,75 \cdot V_e$

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T_{\min} [m] = μ μ

V_e [km/h] = μ

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μ μ μ : $Ds_{\max} = 0,3 / V_e^2$

Ds_{\max} [m/ m] = .

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- $V_e > 70$ km/ h, 30 m

- $V_e = 70 \text{ km/h}, 15 \text{ m}$

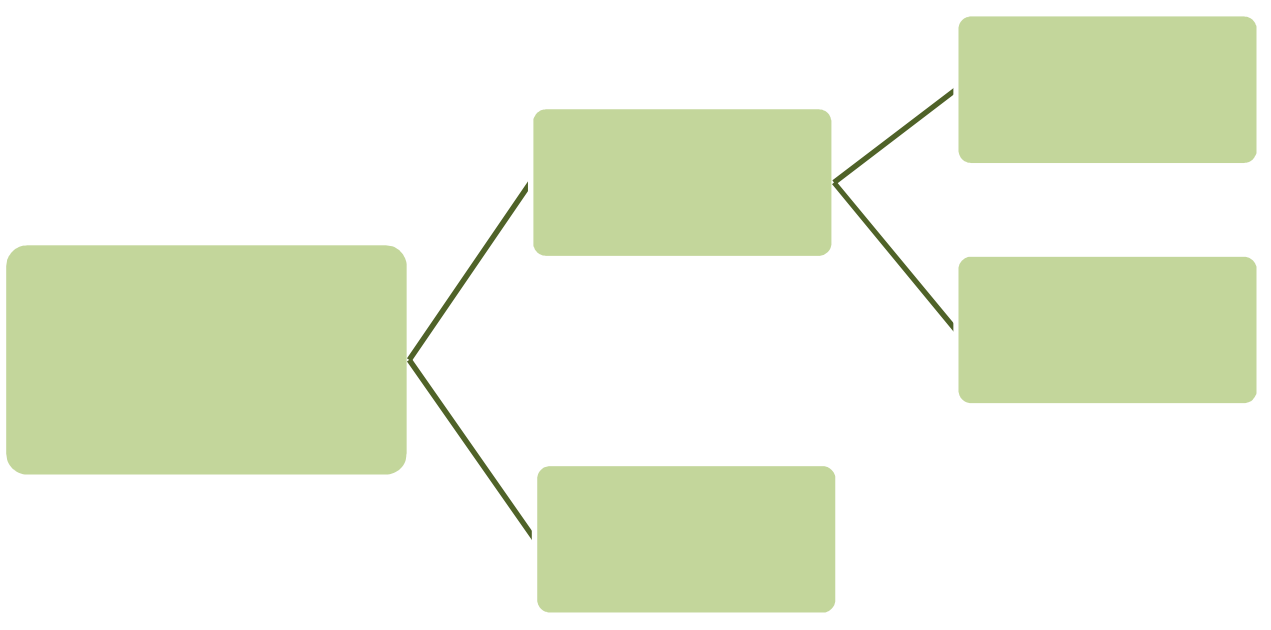
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μ N. Metropolis & S. Ulam 1949 μ "

μ Monte Carlo" Journal of the American Statistics Association

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Monte Carlo

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Monte Carlo

- 1: μ , $f(x_1, x_2, \dots, x_n)$.
- 2: μ , $x_{i1}, x_{i2}, \dots, x_{in}$ $y_{i1}, y_{i2}, \dots, y_{in}$.
- 3: μ f_i .
- 4: μ μ^2 μ^3 $i = 1$ n . Monte Carlo

$1/\sqrt{N}$

(chromosome), (gene), (loci), (allele), (phenotype),
 (crossover), (mutate), (objective, fitness function)

Friedberg 1958
 Fortran

Holland 1975. Holland
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Goldberg (1989) Michalewicz (1996)

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(Roulette Wheel Selection)

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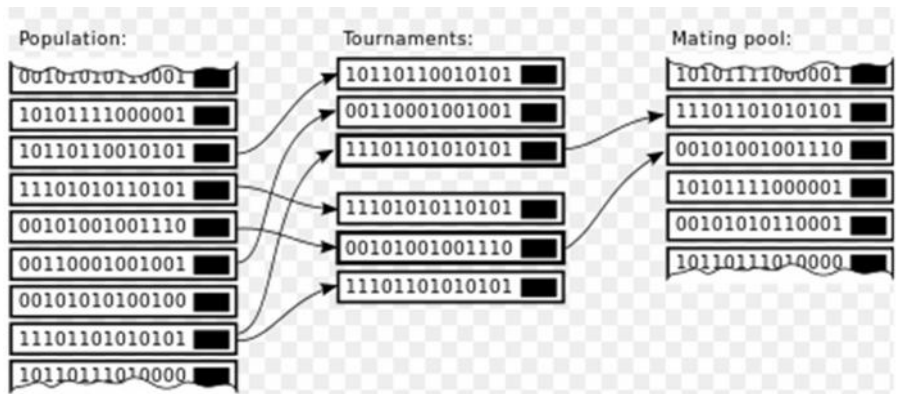
(Linear Ranking Selection)

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 $p_i = \frac{2 * (n - j)}{n * (n - 1)}$ n μ j μ i

(Rank selection)

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 μ μ (μ Tournament Selection)
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4 Python

4.1 Python

Python is a high-level, general-purpose programming language that is interpreted, interactive, dynamically typed, and object-oriented. It is open source and was created by Guido van Rossum in 1991. Python is designed to be easy to learn and use, and it is used in a wide variety of applications, including web development, data analysis, and artificial intelligence. Python is a multi-paradigm language, supporting procedural, object-oriented, and functional programming styles. It has a rich standard library and a large ecosystem of third-party packages. Python is cross-platform and runs on a variety of operating systems, including Windows, Linux, and macOS. It is also used in scientific computing and data science, where its powerful data manipulation and visualization libraries are highly valued. Python is a popular choice for beginners and experienced programmers alike, and it is widely used in industry and academia. Python is known for its readability and simplicity, which makes it a great language for learning and for writing code quickly. It is also a powerful language that can be used to build complex and scalable applications. Python is a versatile language that can be used in many different ways, and it is constantly evolving to meet the needs of the community. Python is a language that is easy to learn and use, but it is also a language that is powerful and flexible. It is a language that can be used to solve a wide variety of problems, and it is a language that is constantly growing and improving. Python is a language that is worth learning and using, and it is a language that is sure to continue to be popular for many years to come.

4.2 Python

4.2.1 Python

Python is a high-level programming language that is interpreted and interactive. It is designed to be easy to learn and use, and it is used in a wide variety of applications, including web development, data analysis, and artificial intelligence. Python is a multi-paradigm language, supporting procedural, object-oriented, and functional programming styles. It has a rich standard library and a large ecosystem of third-party packages. Python is cross-platform and runs on a variety of operating systems, including Windows, Linux, and macOS. It is also used in scientific computing and data science, where its powerful data manipulation and visualization libraries are highly valued. Python is a popular choice for beginners and experienced programmers alike, and it is widely used in industry and academia. Python is known for its readability and simplicity, which makes it a great language for learning and for writing code quickly. It is also a powerful language that can be used to build complex and scalable applications. Python is a versatile language that can be used in many different ways, and it is constantly evolving to meet the needs of the community. Python is a language that is easy to learn and use, but it is also a language that is powerful and flexible. It is a language that can be used to solve a wide variety of problems, and it is a language that is constantly growing and improving. Python is a language that is worth learning and using, and it is a language that is sure to continue to be popular for many years to come.

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4.2.4

$$(y - y_0) = \frac{y_1 - y_0}{x_1 - x_0} * (x - x_0).$$

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V_e [km/h]	S_{max} [%] για τις οδούς της ομάδας			
	Α			Β (πλήν ΒΙ)
	πεδινά εδάφη	λοφώδη εδάφη	ορεινά εδάφη	όλες οι κατηγορίες εδαφών
50	7 (8)	8 (9)	10 (11)	8 (12)
60	6 (8)	7 (9)	9 (10)	7 (10)
70	5 (7)	6 (8)	8 (9)	6 (9)
80	4 (6)	5 (7)	7 (9)	5 (7)
90	4 (5)	5 (6)	7 (8)	-
100	3 (5)	4 (6)	6 (8)	-
110	3 (5)	4 (6)	5 (6)	-
120	3 (5)	4 (6)	-	-
130	3 (4)	-	-	-

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- $s_2 < s_1$, μ .
 - b) $\mu \mu \mu \mu$ s_1 ():
 - $s_2 > s_1$, μ .
 - $s_2 < s_1$, μ .
- μ , μ $s_2 > s_1$,
 $s_2 < s_1$.(2013)

μ μ -

V_e [km/h]	H_w min [m]
50	1.350
60	1.900
70	2.500
80	3.300
90	4.200
100	5.200
110	6.300
120	7.500
130	10.000

3: μ μ μ μ

μ		μ				
200	50	1	16790.38	16979.33	51	178.82
		2	16438	17153.57	51	391.13
		3	16184.91	17474.24	51	477.84
		4	12745.95	17883.89	51	1267.86
		5	16725.73	19059.66	51	1265.01
		6	17273.45	19958.22	51	1764.6
		7	17671.24	21384.69	51	1756.15
		8	17046.81	23289.13	51	2452.21
		9	20252.02	25886.48	51	2671.82
	100	1	16784.52	17001.21	74	179.34
		2	16504.48	17077.56	74	264.74
		3	15830.15	17444.49	71	700.52
		4	16725.14	18393.62	64	830.36
		5	16570.59	20177.77	55	1682.51
		6	19962.59	23593.77	55	2004.03
		7	21311.54	27961.55	55	3853.8
		8	13414.41	34775.04	66	10163.54
		9	29575.43	49168.36	55	9214.9

μ		μ				
2000	50	1	16782.75	16816.79	68	24.92
		2	15957.05	16607.59	39	234.62
		3	15541.55	16544.77	12	499.67
		4	15111.38	16630.49	12	545.83
		5	15534.86	16552.63	12	690.08
		6	12419.77	15738.96	50	1405.23
		7	15286.34	17371	8	1283.26
		8	16631.67	19385.4	8	1726.07
		9	17708.81	20135.26	8	1572.22
	100	1	16784.25	16818.5	51	31.31
		2	16479.54	16767.93	51	125.24
		3	15869.39	16754.59	51	312.2
		4	16149.27	17039.37	51	414.27
		5	15568.3	17543.29	51	832.59
		6	16276.76	19209.98	51	1205.56
		7	17161.22	22517.73	51	2458.33
		8	17375.89	26644.53	51	3299.11
		9	25492.6	35612.05	18	5523.02


```

import multiprocessing
from multiprocessing import Pool

def monteCarlo(xth, y, a):
    """Using Monte Carlo find optimum grade points."""
    Point.setGround(xth, y)
    ntries = a*2 * ntriesperdim
    pomin = Point(a)

    nprocesses = multiprocessing.cpu_count()
    ntries1 = ntries//nprocesses
    pool = multiprocessing.Pool(nprocesses)

    argslst = [(a, ntries1)] * nprocesses
    for po1 in pool.imap_unordered(doSome, argslst):
        if po1.emb < pomin.emb:
            pomin = po1
    return pomin

if __name__ == '__main__':
    μ : multiprocessing

```

```

def monteCarlo(xth, y, a):
    """Using Monte Carlo find optimum grade points."""
    Point.setGround(xth, y)
    ntries = a*2 * ntriesperdim
    pomin = Point(a)

    nprocesses = multiprocessing.cpu_count()
    ntries1 = ntries//nprocesses
    pool = multiprocessing.Pool(nprocesses)

    argslst = [(a, ntries1)] * nprocesses
    for po1 in pool.imap_unordered(doSome, argslst):
        if po1.emb < pomin.emb:
            pomin = po1
    return pomin

μ : multiprocessing

```


$$\begin{bmatrix} y_1 \\ y_2 \\ \vdots \\ y_k \\ y_{k+1} \\ y_{k+2} \\ \vdots \\ y_N \end{bmatrix} = \begin{bmatrix} x_1 & 1 & 0 \\ x_2 & 1 & 0 \\ \vdots & \vdots & \vdots \\ x_k & 1 & 0 \\ u_1 & 1 & x_{k+1} - u_1 \\ u_1 & 1 & x_{k+2} - u_1 \\ \vdots & \vdots & \vdots \\ u_1 & 1 & x_N - u_1 \end{bmatrix} \cdot \begin{bmatrix} b_1 \\ a_1 \\ a_2 \\ a_3 \\ a_4 \\ \vdots \\ a_n \\ a_{n+1} \end{bmatrix} \quad [B] = [A] \cdot [X]$$

$x = \text{random.rand}(n) * L + u_1 + 10$
 $H = \text{random.rand}(n, [0, 1])$
 $V = \text{Cramer}(x, H, L, u_1)$
 $nAnim = \text{Anim}(x, H, L, u_1)$
 $nAnimCompute() = \text{AnimCompute}(x, H, L, u_1, nValmax, (26), (5), (20))$
 $(x_2 - x_1) * 10^n \cdot 2^{t_i} - 1$
 $nValmax$

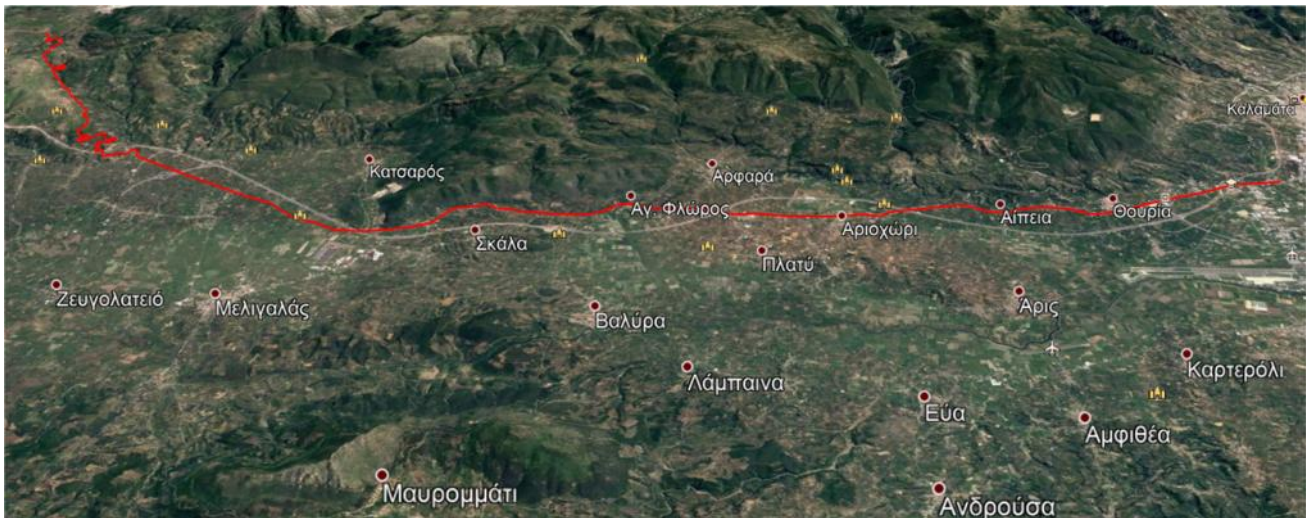
5.1.1

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 μ 3+ 403.71 μ -
 μ $V_e = 120$ km/ h.
 μ - , $h_w = 7500$
 $h_k = 15000.$ μ μ μ 13284.98 m²
 μ .

X.Θ.	Y
-1+162.71	88.14
-0+202.27	64.28
0+430.97	70.43
0+845.97	54.09
1+703.01	50.38
2+427.66	36.27
2+760.72	42.50
3+069.53	33.91
3+403.71	34.00

5.1.2

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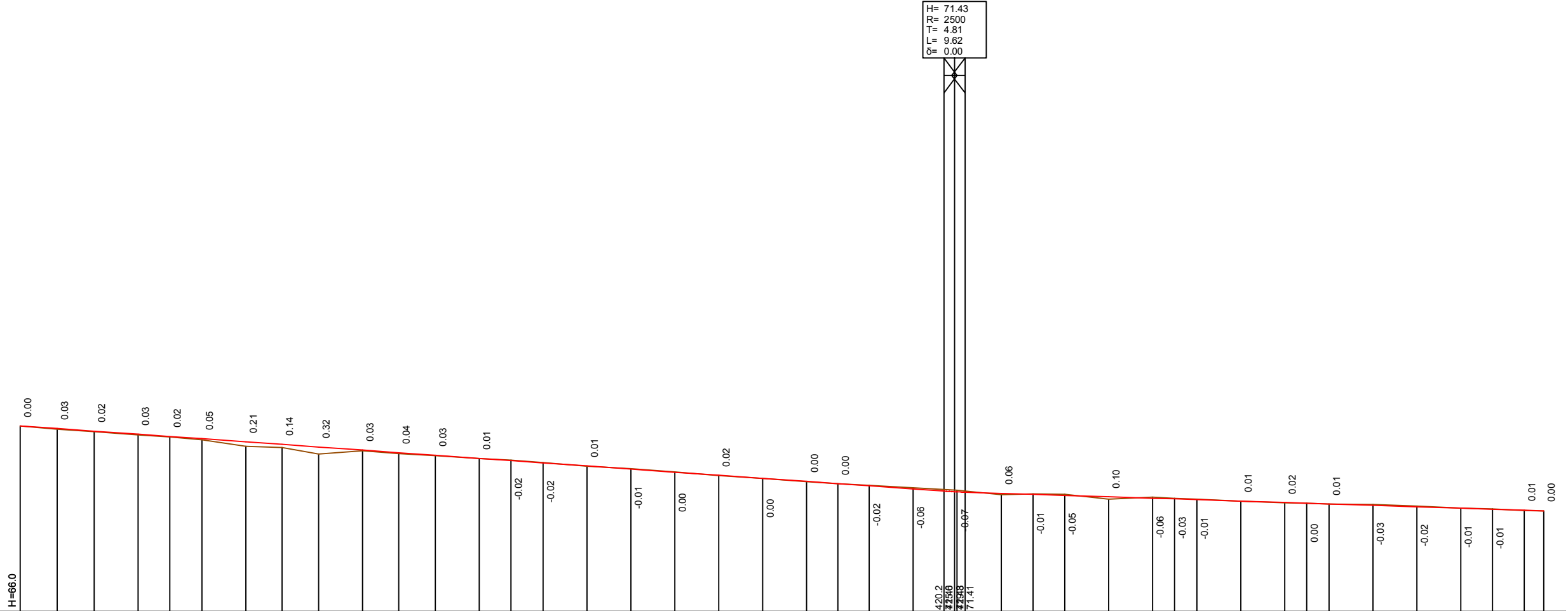
15: μ

μ μ , μ 692.91 m, μ , μ
 , μ - μ
 μ $V_e = 80 \text{ km/h.}$ μ
 μ - , $h_w = 2500$
 $h_k = 4500.$ μ μ μ 25.64m^2
 μ μ μ

Χ.Θ.	Υ
0+000.00	74.43
0+424.97	71.43
0+692.91	70.57

ΕΠ. Οδός Νομού Μεσσηνίας

ΚΛΙΜΑΚΑ ΥΨΩΝ = 1/200
 ΚΛΙΜΑΚΑ ΜΗΚΩΝ = 1/2000

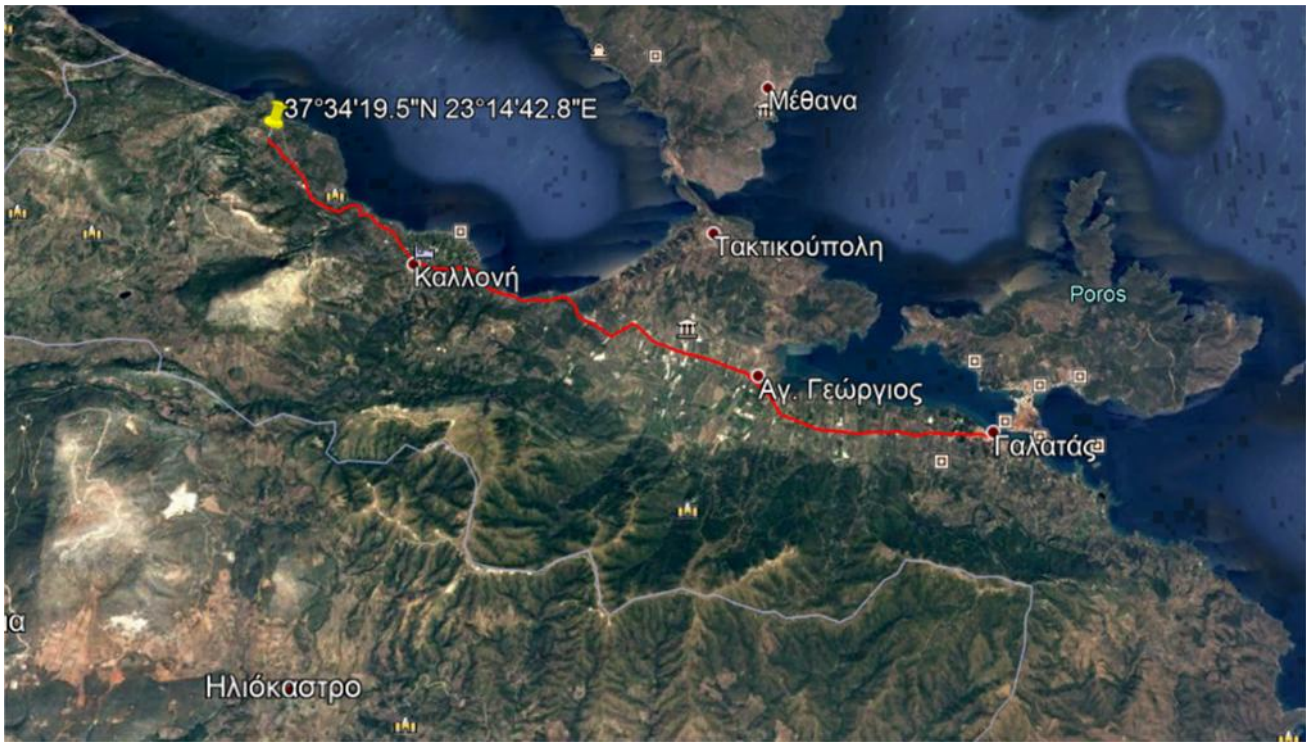


ΥΨΟΜΕΤΡΑ ΕΡΥΘΡΩΝ	74.43	74.31	74.19	74.05	73.95	73.85	73.71	73.59	73.47	73.33	73.21	73.10	72.96	72.85	72.75	72.61	72.47	72.33	72.19	72.05	71.90	71.80	71.70	71.56	71.43	71.36	71.32	71.27	71.20	71.14	71.11	71.08	71.01	70.95	70.92	70.88	70.82	70.76	70.69	70.64	70.60	70.57						
ΥΨΟΜΕΤΡΑ ΕΔΑΦΟΥΣ	74.43	74.28	74.17	74.02	73.93	73.80	73.50	73.45	73.15	73.30	73.17	73.07	72.95	72.87	72.77	72.60	72.48	72.33	72.17	72.05	71.90	71.80	71.72	71.62	71.50	71.30	71.33	71.32	71.10	71.20	71.14	71.11	71.09	71.00	70.93	70.92	70.87	70.85	70.78	70.70	70.65	70.59	70.57					
ΑΡΙΘΜΗΣΗ ΔΙΑΤΟΜΩΝ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42						
ΑΠΟΣΤΑΣΕΙΣ ΜΕΤΑΞΥ	16.8	16.8	20.0	14.5	14.5	20.0	16.5	16.5	20.0	16.5	16.5	20.0	14.5	14.5	20.0	20.0	20.0	20.0	20.0	20.0	14.2	14.2	20.0	20.0	20.0	14.4	14.4	20.0	20.0	10.0	10.0	20.0	20.0	10.1	10.0	20.0	20.0	20.0	20.0	14.5	14.4	8.8						
ΑΠΟΣΤΑΣΕΙΣ ΑΠΟ ΑΡΧΗΣ	0.0	16.8	33.6	53.6	68.1	82.6	102.6	119.2	135.7	155.7	172.2	188.8	208.8	223.3	237.8	257.8	277.8	297.8	317.8	337.8	357.8	372.0	386.2	406.2	426.2	446.2	460.6	475.1	495.1	515.1	525.1	535.2	555.2	575.2	585.2	595.3	615.3	635.3	655.3	669.7	684.2	692.9						
ΧΙΛΙΟΜΕΤΡΗΣΗ	X	0																																														
ΕΥΘΥΓΡΑΜΜΙΕΣ-ΚΑΜΠΥΛΕΣ																																																
ΤΟΞΑ - ΚΛΙΣΕΙΣ																																																

-0.7 %
420.16

-0.3 %
263.13

5.1.3

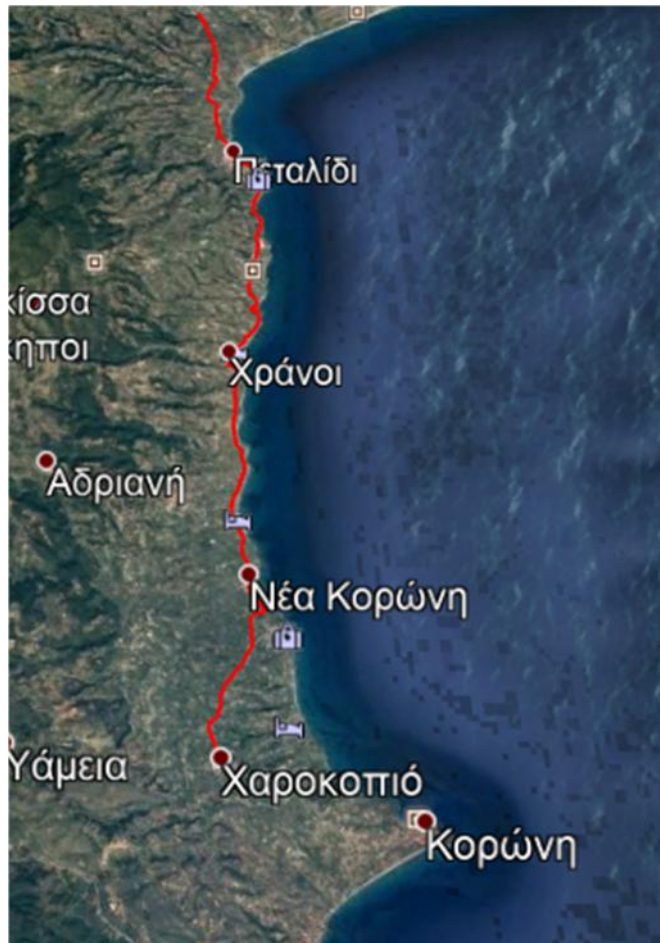


16:

$\mu \mu , \mu$ 1173.4 m, μ
 μ 5+ 407.23 μ 6+ 580.63
 μ - V, μ $V_e =$
 60 km/ h. μ μ - ,
 $h_w = 1900$ $h_k = 3000.$ μ
 $\mu \mu$ 506.57 m² μ .

Χ.Θ.	Υ
5+407.23	13.78
6+077.44	7.92
6+186.51	10.57
6+580.63	5.84

5.1.4 μ -



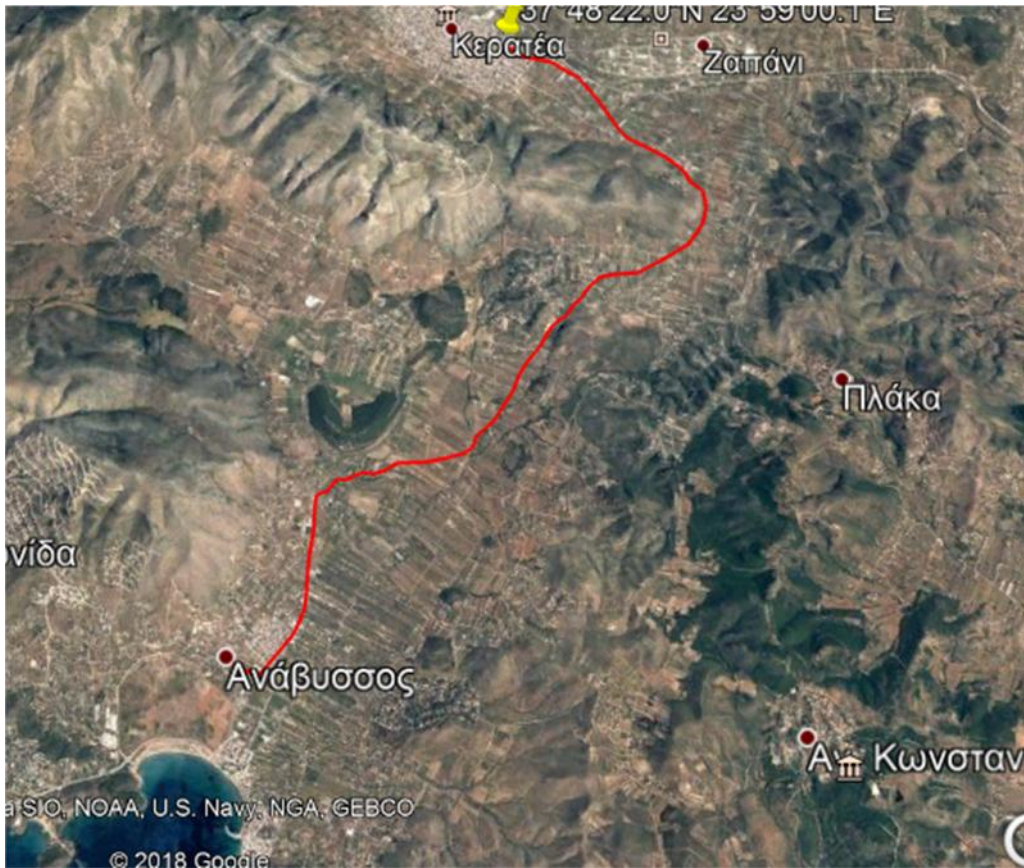
17:

μ -

$\mu \mu , \mu$ 1000 m, $\mu \mu$
 μ 3+ 000.00 μ 4+ 000.00
 μ - , μ $V_e =$
 70 km/ h. μ - ,
 $h_w = 2500$ $h_k = 4500.$ μ
 $\mu \mu$ 820,23 m² μ .

Χ.Θ.	Υ
3+000.00	11.27
3+154.40	4.57
3+450.16	19.90
4+000.00	10.00

5.1.5

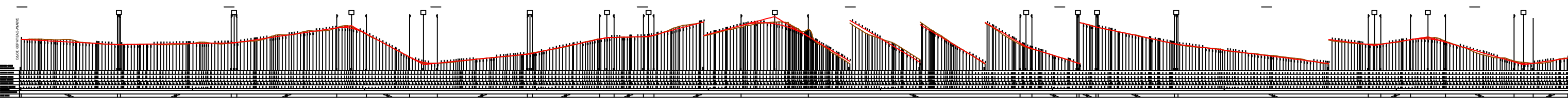


18: μ μ -

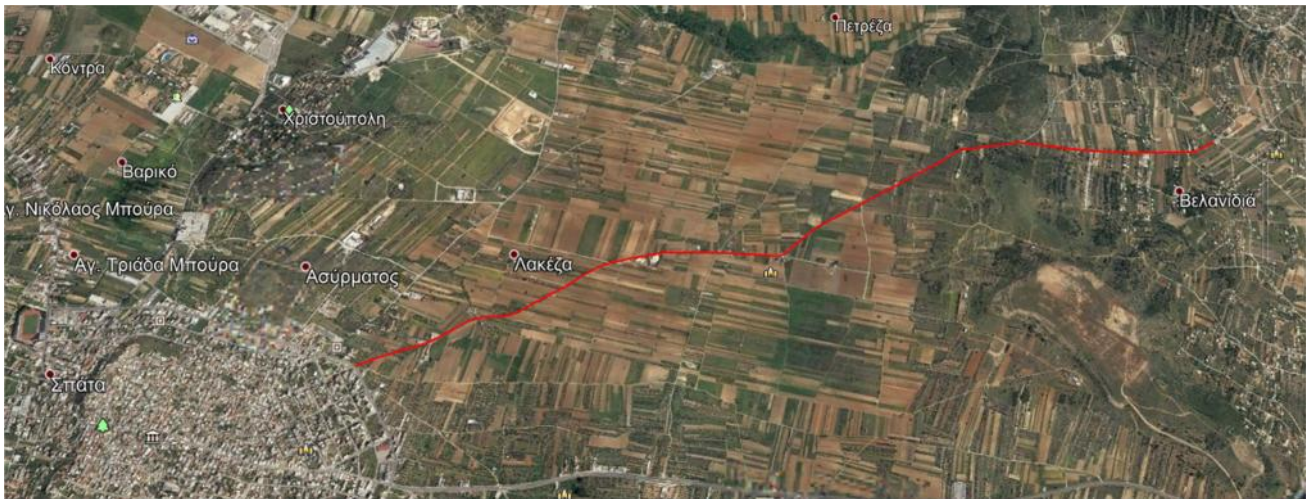
$\mu \mu , \mu$ 8994.99 m, μ
 μ 0+ 000.00 μ 8+ 994.99
 μ - μ $V_e = 70$
 km/ h. μ μ - ,
 $h_w = 1900$ $h_k = 3000.$ μ
 $\mu \mu$ 3958.18 m² μ .

Χ.Θ.	Υ
0+000.00	148.15
0+568.23	145.05
1+238.02	146.09
1+920.44	156.10
2+338.79	133.41
2+958.07	139.65
3+405.51	149.19
3+648.73	149.80
4+381.65	169.51

Χ.Θ.	Υ
5+843.12	81.88
6+144.53	72.27
6+256.53	69.29
6+716.60	59.39
7+870.07	44.65
8+180.81	49.57
8+736.96	33.31
8+994.99	37.13



5.1.6

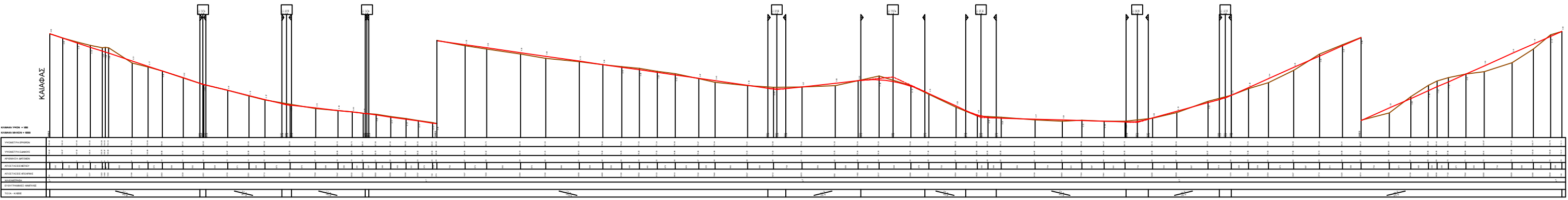


19 :

μ , μ 4014.80 m, μ
 0+ 000.00 μ 4+ 014.80 μ
 μ $V_e = 70$ km/ h. μ μ μ
 1382.03 m² μ

Χ.Θ.	Υ
0+000.00	109.46
0+406.53	96.08
0+628.54	90.64
0+841.97	88.31
1+930.21	72.70
2+238.48	76.04
2+472.49	65.29
2+887.35	64.00
3+121.13	70.51
4+014.80	110.11

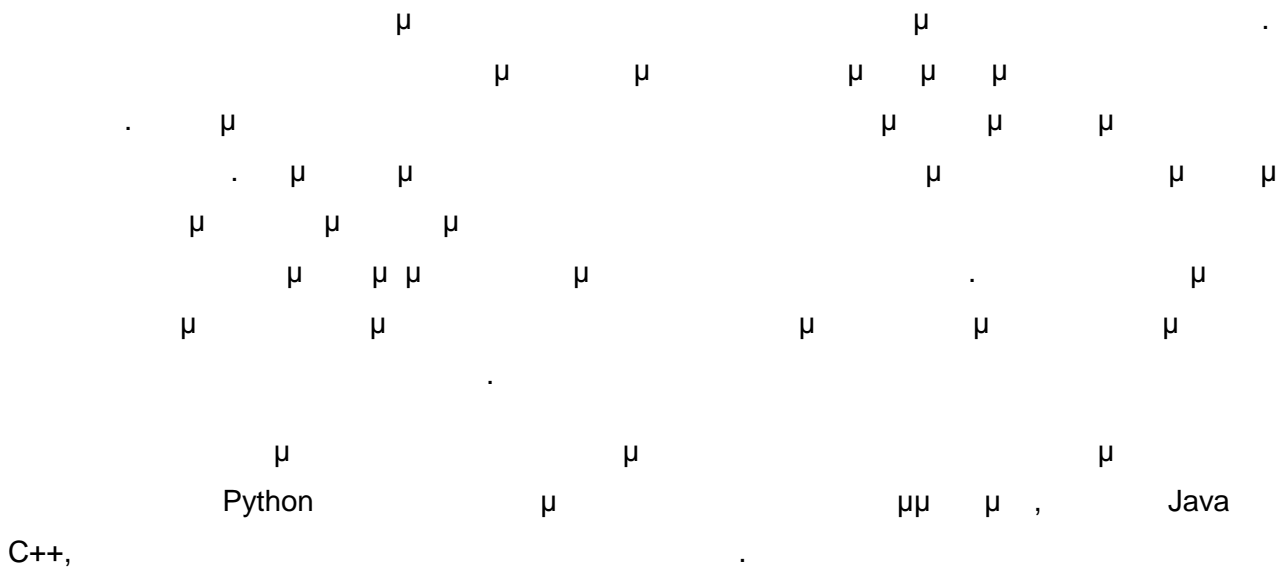
ΚΑΙΛΑΦΑΣ



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ΥΠΟΚΑΤΑΣΤΑΣΗ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
ΑΡΧΙΤΕΚΤΟΝΙΚΗ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
ΑΡΧΙΤΕΚΤΟΝΙΚΗ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
ΑΡΧΙΤΕΚΤΟΝΙΚΗ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
ΑΡΧΙΤΕΚΤΟΝΙΚΗ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
ΑΡΧΙΤΕΚΤΟΝΙΚΗ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
ΑΡΧΙΤΕΚΤΟΝΙΚΗ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
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ΑΡΧΙΤΕΚΤΟΝΙΚΗ	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30	31	32	33	34	35	36	37	38	39	40	41	42	43	44	45	46	47	48	49	50	51	52	53	54	55	56	57	58	59	60	61	62	63	64	65	66	67	68	69	70	71	72	73	74	75	76	77	78	79	80	81	82	83	84	85	86	87	88	89	90	91	92	93	94	95	96	97	98	99	100
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 », μ , ,
 , .
 .. (2013), « μ μ μ μ NURBS
 (Non-Uniform Rational Basis Spline)», μ , ,
 , .

Al-Sayed A. Al-Sobky, (2015), « Genetic Algorithms for Highway Vertical Alignment Optimization », World Applied Sciences Journal 29 (7): 884-891, Cairo Egypt

Bäck T. and Schwefel H.-P.. (1993). "An Overview of Evolutionary Algorithms for Parameter Optimization", *Evol. Comput.*, vol. 1, no. 1, pp. 1–23.

BUREAU OF DESIGN AND ENVIRONMENT, (2010), BUREAU OF DESIGN AND ENVIRONMENT MANUAL, "Vertical Alignment", Chapter 33, Illinois

Coley D. A., (1999), "An Introduction to Genetic Algorithms for Scientists and Engineers", WORLD SCIENTIFIC.

D. E. (David E. Goldberg and D. E.), (1989), "Genetic algorithms in search, optimization, and machine learning", Addison-Wesley Longman Publishing Co., Inc..

Darwin C., (1859), "On the Origin of the Species", vol. 5.

Al-Sayed A. Al-Sobky, (2014), "An Optimization Approach for Highway Vertical Alignment Using the Earthwork Balance Condition", *World Applied Sciences Journal* 29 (7): 884-891, Cairo Egypt

Bäck T. and Schwefel H.-P.. (1993). "An Overview of Evolutionary Algorithms for Parameter Optimization", *Evol. Comput.*, vol. 1, no. 1, pp. 1–23.

BUREAU OF DESIGN AND ENVIRONMENT, (2010), BUREAU OF DESIGN AND ENVIRONMENT MANUAL, "Vertical Alignment", Chapter 33, Illinois

Coley D. A., (1999), "An Introduction to Genetic Algorithms for Scientists and Engineers", WORLD SCIENTIFIC.

D. E. (David E. Goldberg and D. E.), (1989), "Genetic algorithms in search, optimization, and machine learning", Addison-Wesley Longman Publishing Co., Inc..

Darwin C., (1859), "On the Origin of the Species", vol. 5.

- Dessalegn Amenu Hirpa, (2014), "Simultaneous optimization of vertical and horizontal road alignments", The University Of British Columbia.
- Davey N., Dunstall S., Halgamuge S., (2017), "Optimal road design through ecologically sensitive areas considering animal migration dynamics", *Transportation Research, Part C* 77, pp. 478–494
- Davis L. D. and Mitchell M., (1991), "Handbook of Genetic Algorithms", VAN NOSTRAND REINHOLD, vol. 15, no. 1, pp. 4–6.
- Drezner Z. and Drezner T., (2005), "Genetic Algorithms", *Biomimetics*.
- Easa S. M., (1987), "SELECTION OF ROADWAY GRADES THAT MINIMIZE EARTHWORK COST USING LINEAR PROGRAMMING", *Rex.-A Vol. 2, No. 2*, pp 121-136., Ontario
- Fan Tao, (2004), "BI-LEVEL GENETIC ALGORITHM APPROACH FOR 3D ROAD ALIGNMENT OPTIMIZATION", Thesis for the degree of Master of Engineering Department of Civil Engineering, National University of Singapore
- Friedberg R. M., (1958), "A learning machine: Part I", *IBM J. Res. Dev.*, vol. 2, no. 1, pp. 2–13.
- Fwa, T. F., Chan, W. T., & Sim, Y. P. (2002, September). Optimal Vertical Alignment Analysis for Highway Design. *Journal of Transportation Engineering*, 128(5), pp. 395–402.
- Goktepe A. B., Lav A. H. and Altun S., (2009), "Method for optimal vertical alignment of highways", *Proceedings of the Institution of Civil Engineers, Transport* 162, Issue TR4, Pages 177–188
- Holland J., (1975), *Adaption in Natural and Artificial Systems*, vol. 11.
- Jong J.-C. (1998). *Optimizing Highway Alignments with Genetic Algorithms*. PhD dissertation, University of Maryland, Department of Civil Engineering, College Park, MD.
- Kang M.-W., Schonfeld P., & Jong, J.-C. (2007, March). Highway Alignment Optimization through Feasible Gates. *Journal of Advanced Transportation*, 41(2), pp. 115-144.
- Kang M. W., Shariat S., (2013), "New highway geometric design methods for minimizing vehicular fuel consumption and improving safety", *Transportation Research Part C Emerging Technologies*
- Landau D. P., Binder K.,(2009), "A Guide to Monte Carlo Simulations in Statistical Physics", Third Edition, Cambridge University Press
- Lee W. , Kim H. –Y., (2005), "Genetic Algorithm Implementation in Python", *Proceedings of the Fourth Annual ACIS International Conference on Computer and Information Science (ICIS'05)*

Michalewicz Z., (1996), "Genetic Algorithms + Data Structures = Evolution Programs,"
Computational Statistics & Data Analysis, vol. 24, no. 3, pp. 372–373

Mitchell M., (1998), "An Introduction to Genetic Algorithms (Complex Adaptive Systems),"
MIT Press. no. 6, p. 221, 1996.

Press W., Teukolsky S., Vetterling W., Flannery B., (2007), "Numerical recipes. The art of scientific
computing", Third edition, Cambridge University Press

Transit New Zealand, (2002), "STATE HIGHWAY GEOMETRIC DESIGN MANUAL
SECTION 5: VERTICAL ALIGNMENT", Section 5, New Zealand

<http://www.anadelta.com>

<http://www.diolkos3d.com>

<http://www.google.com>

<http://www.imola.odos.gr>

<http://www.mathesis.gr>

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X.Θ.	Y	X.Θ.	Y	X.Θ.	Y
-1+162.71	88.14	-0+776.57	80.00	-0+389.86	78.00
-1+156.23	89.00	-0+766.64	81.00	-0+384.63	77.80
-1+150.48	90.00	-0+755.00	82.00	-0+374.23	77.40
-1+143.53	91.00	-0+746.94	82.53	-0+363.83	77.00
-1+133.89	92.00	-0+739.65	83.00	-0+344.94	76.00
-1+127.30	93.00	-0+732.64	84.00	-0+333.67	75.00
-1+120.71	94.00	-0+725.30	85.00	-0+329.11	74.00
-1+104.92	95.00	-0+712.91	86.00	-0+324.54	73.00
-1+086.81	95.00	-0+707.30	87.00	-0+316.25	71.99
-1+078.21	95.00	-0+695.96	88.00	-0+310.41	71.00
-1+066.75	94.00	-0+686.51	89.00	-0+303.19	70.00
-1+055.81	93.50	-0+678.88	90.00	-0+295.95	69.00
-1+044.87	93.00	-0+668.08	91.00	-0+288.71	68.00
-1+030.63	92.00	-0+658.71	92.00	-0+281.40	67.00
-1+020.14	91.50	-0+647.55	93.00	-0+271.24	66.00
-1+009.65	91.00	-0+631.83	94.00	-0+265.31	65.00
-0+999.58	90.50	-0+612.04	94.00	-0+259.37	64.00
-0+989.51	90.00	-0+601.31	94.00	-0+252.84	63.00
-0+973.73	89.00	-0+590.59	94.00	-0+244.98	62.00
-0+958.33	88.00	-0+580.42	93.00	-0+241.41	62.00
-0+948.05	87.00	-0+572.73	92.00	-0+229.26	62.00
-0+937.72	86.00	-0+564.09	91.00	-0+217.12	62.00
-0+927.80	85.00	-0+557.64	90.00	-0+201.29	61.00
-0+914.94	84.00	-0+551.80	89.00	-0+194.17	60.00
-0+908.47	83.00	-0+542.14	88.00	-0+190.17	59.00
-0+900.36	82.00	-0+532.28	87.00	-0+186.18	58.00
-0+888.70	81.00	-0+522.39	86.00	-0+182.18	57.00
-0+875.73	80.00	-0+515.50	85.00	-0+170.11	56.42
-0+870.85	79.00	-0+504.89	84.00	-0+161.42	56.00
-0+865.96	78.00	-0+498.60	83.53	-0+158.12	55.97
-0+861.56	78.00	-0+491.62	83.00	-0+139.24	55.78
-0+858.21	79.00	-0+480.01	82.39	-0+119.41	55.59
-0+855.15	80.00	-0+472.52	82.00	-0+099.78	55.40
-0+842.20	80.56	-0+461.32	81.64	-0+081.27	55.22
-0+832.16	81.00	-0+451.21	81.32	-0+069.97	55.11
-0+822.57	81.00	-0+441.10	81.00	-0+058.67	55.00
-0+811.21	81.00	-0+431.95	80.00	-0+055.23	54.00
-0+799.29	80.00	-0+423.26	79.49	-0+051.68	53.00
-0+796.46	79.00	-0+414.88	79.00	-0+047.53	52.00
-0+786.29	79.00	-0+404.11	78.57	-0+038.42	52.00

X.Ø.	Y	X.Ø.	Y	X.Ø.	Y
-0+033.77	53.00	0+396.43	74.00	0+848.56	54.00
-0+028.87	54.00	0+405.59	74.37	0+851.26	53.00
-0+023.96	55.00	0+421.54	75.00	0+865.53	53.00
-0+010.82	55.52	0+433.05	75.00	0+877.86	53.00
0+000.00	55.95	0+444.56	75.00	0+880.18	53.00
0+001.32	56.00	0+456.13	74.00	0+887.07	53.00
0+015.92	57.00	0+465.79	73.00	0+905.03	53.60
0+030.18	58.00	0+473.30	72.00	0+916.77	54.00
0+040.16	59.00	0+474.38	71.88	0+926.76	55.00
0+046.77	60.00	0+482.65	71.00	0+944.15	55.00
0+051.85	61.00	0+495.52	70.00	0+962.44	55.00
0+056.28	62.00	0+505.55	69.50	0+977.46	55.00
0+060.73	63.00	0+515.57	69.00	0+984.58	55.00
0+065.52	64.00	0+525.27	68.00	1+000.57	55.00
0+070.45	65.00	0+531.66	67.49	1+011.36	55.00
0+075.11	66.00	0+537.75	67.00	1+022.15	55.00
0+084.52	67.00	0+551.97	66.00	1+032.18	54.50
0+096.18	68.00	0+554.16	66.00	1+042.20	54.00
0+099.01	68.00	0+571.12	65.00	1+052.23	53.50
0+101.43	68.00	0+590.56	64.00	1+062.27	53.00
0+108.35	69.00	0+607.72	63.41	1+078.03	52.00
0+114.08	69.19	0+619.51	63.00	1+093.83	52.00
0+132.76	69.81	0+632.51	62.36	1+097.68	52.00
0+138.69	70.00	0+639.77	62.00	1+116.55	52.00
0+156.45	71.00	0+650.73	61.69	1+119.20	53.00
0+172.00	71.14	0+668.92	61.17	1+120.21	54.00
0+190.39	71.00	0+675.01	61.00	1+121.25	55.00
0+209.40	71.00	0+685.70	60.00	1+128.63	55.00
0+219.05	71.00	0+688.55	60.00	1+136.15	54.00
0+227.43	70.00	0+700.63	59.00	1+156.09	53.68
0+237.19	69.57	0+706.61	58.72	1+174.21	53.40
0+249.77	69.00	0+720.15	58.00	1+193.99	53.08
0+258.21	68.00	0+735.80	57.00	1+199.34	53.00
0+268.16	67.00	0+740.87	57.00	1+212.48	52.68
0+270.02	67.00	0+751.30	56.50	1+231.12	52.23
0+285.44	68.00	0+761.72	56.00	1+240.73	52.00
0+296.22	69.00	0+777.72	55.57	1+250.12	52.00
0+299.85	69.00	0+790.63	55.23	1+263.23	52.00
0+312.30	69.00	0+799.24	55.00	1+269.37	52.00
0+323.33	70.00	0+808.87	54.52	1+289.02	52.00
0+330.46	70.48	0+819.16	54.00	1+308.24	52.00
0+338.14	71.00	0+821.47	54.00	1+327.29	52.00
0+353.29	72.00	0+827.89	54.00	1+345.81	52.00
0+370.90	73.00	0+842.52	54.00	1+364.99	51.77
0+385.69	73.58	0+845.26	54.00	1+380.65	52.00

X.Ø.	Y	X.Ø.	Y	X.Ø.	Y
1+391.73	52.00	1+953.09	44.00	2+506.16	36.00
1+402.81	52.00	1+955.75	44.00	2+511.81	36.00
1+422.31	52.00	1+966.26	44.00	2+514.35	37.00
1+433.62	52.00	1+976.77	44.00	2+524.45	37.50
1+444.93	52.00	1+990.77	43.00	2+534.55	38.00
1+460.77	51.30	1+993.25	43.00	2+553.32	38.70
1+467.61	51.00	2+009.29	43.00	2+561.09	39.00
1+479.63	51.00	2+028.64	42.00	2+562.23	39.00
1+482.67	51.00	2+032.78	42.00	2+571.39	39.46
1+490.30	51.00	2+050.22	42.00	2+582.24	40.00
1+499.36	51.00	2+056.59	42.00	2+589.77	40.41
1+517.84	51.00	2+070.04	42.00	2+600.63	41.00
1+537.02	51.00	2+088.72	42.00	2+606.89	41.00
1+556.72	51.00	2+093.82	42.00	2+622.37	41.64
1+576.31	51.00	2+097.09	42.00	2+631.36	42.00
1+595.56	50.91	2+099.85	42.00	2+640.27	42.00
1+615.11	51.00	2+108.38	42.00	2+653.03	42.00
1+633.46	51.00	2+121.03	42.00	2+661.19	42.12
1+652.68	51.00	2+131.13	42.00	2+680.40	42.40
1+671.29	51.00	2+142.38	42.00	2+700.34	42.69
1+691.11	50.73	2+150.53	41.91	2+710.87	42.85
1+701.76	51.00	2+168.60	41.70	2+721.39	43.00
1+704.72	52.00	2+188.29	41.47	2+733.69	43.00
1+710.46	52.00	2+207.85	41.25	2+746.03	42.64
1+726.16	52.00	2+218.81	41.13	2+757.92	42.28
1+728.21	51.00	2+229.76	41.00	2+766.90	42.00
1+730.23	50.00	2+244.65	40.65	2+774.21	42.00
1+731.31	50.00	2+263.33	40.24	2+776.18	42.00
1+738.08	50.00	2+274.59	40.00	2+787.08	41.50
1+749.74	49.74	2+282.37	39.80	2+797.97	41.00
1+768.32	49.32	2+301.65	39.33	2+802.82	41.00
1+782.63	49.00	2+315.94	39.00	2+813.49	40.54
1+791.27	49.00	2+327.63	38.56	2+826.00	40.00
1+798.06	49.00	2+344.24	38.00	2+832.92	39.76
1+806.81	49.00	2+355.25	37.90	2+843.71	39.38
1+815.36	49.00	2+366.26	37.80	2+854.49	39.00
1+825.65	48.68	2+384.74	37.63	2+864.76	38.50
1+845.43	48.00	2+403.91	37.47	2+875.03	38.00
1+861.62	47.00	2+421.91	37.33	2+883.57	38.00
1+881.25	46.00	2+439.93	37.19	2+893.62	37.00
1+901.24	45.22	2+458.14	37.02	2+903.74	36.77
1+906.97	45.00	2+463.21	37.00	2+917.12	36.45
1+919.50	44.71	2+476.98	37.00	2+935.04	36.00
1+934.64	44.32	2+496.09	37.00	2+939.43	36.00
1+950.53	44.00	2+503.30	37.00	2+958.91	36.00

X.Ø.	Y
2+974.18	35.40
2+984.17	35.00
2+989.14	35.00
3+001.40	35.00
3+009.92	35.00
3+020.36	35.00
3+030.80	35.00
3+042.50	35.00
3+054.19	35.00
3+067.45	35.00
3+077.69	35.00
3+081.94	35.00
3+099.73	35.00
3+109.03	35.00
3+113.61	35.00
3+131.98	35.00
3+150.81	35.00
3+162.58	35.00
3+174.36	35.00
3+188.44	35.00
3+207.21	35.00
3+225.70	35.00
3+244.00	35.00
3+257.86	35.00
3+263.08	35.00
3+275.19	35.00
3+287.30	35.00
3+296.85	34.90
3+310.11	34.78
3+328.04	34.58
3+347.41	34.38
3+366.55	34.18
3+383.68	34.00
3+397.36	34.00
3+403.71	34.00
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X. Θ.	Y
0+000.00	74.43
0+016.81	74.28
0+033.62	74.17
0+053.62	74.02
0+068.12	73.93
0+082.62	73.80
0+102.62	73.50
0+119.16	73.45
0+135.69	73.15
0+155.69	73.30
0+172.23	73.17
0+188.76	73.07
0+208.76	72.95
0+223.26	72.87
0+237.76	72.77
0+257.76	72.60
0+277.76	72.48
0+297.76	72.33
0+317.76	72.17
0+337.76	72.05
0+357.76	71.90
0+371.98	71.80
0+386.19	71.72
0+406.19	71.62
0+426.19	71.50
0+446.19	71.30
0+460.63	71.33
0+475.08	71.32
0+495.08	71.10
0+515.08	71.20
0+525.13	71.14
0+535.18	71.09
0+555.18	71.00
0+575.18	70.93
0+585.23	70.92
0+595.27	70.87
0+615.27	70.85
0+635.27	70.78
0+655.27	70.70
0+669.72	70.65
0+684.16	70.59
0+692.91	7.57

X.Ø.	Y	X.Ø.	Y	X.Ø.	Y
3+000.00	11.27	3+540.00	18.44	3+980.00	9.87
3+017.18	11.02	3+550.00	18.05	3+986.11	9.90
3+020.00	10.96	3+560.07	17.75	4+000.00	10.00
3+040.00	10.83	3+580.00	17.22		\$
3+042.19	10.83	3+587.04	17.09		
3+060.00	8.23	3+600.00	16.83		
3+067.18	8.20	3+612.05	16.55		
3+080.00	7.98	3+620.00	16.38		
3+100.00	7.80	3+637.04	15.90		
3+120.00	7.66	3+640.00	15.85		
3+140.00	7.60	3+648.39	15.71		
3+160.00	7.49	3+660.00	15.50		
3+180.00	7.50	3+680.00	15.14		
3+200.00	7.49	3+685.62	15.02		
3+220.00	8.19	3+700.00	14.72		
3+240.00	8.55	3+720.00	14.33		
3+243.08	8.63	3+722.85	14.27		
3+260.00	8.08	3+740.00	13.88		
3+270.84	8.68	3+747.42	13.71		
3+280.00	9.12	3+760.00	13.38		
3+298.64	10.21	3+771.98	13.03		
3+300.00	10.34	3+780.00	12.76		
3+313.75	12.40	3+800.00	11.98		
3+316.76	15.75	3+809.21	11.62		
3+320.00	15.71	3+820.00	11.26		
3+340.00	15.86	3+840.00	10.79		
3+356.87	16.26	3+846.44	10.63		
3+360.00	16.29	3+860.00	10.34		
3+380.00	16.96	3+873.19	10.11		
3+400.00	17.51	3+880.00	10.09		
3+415.11	17.93	3+887.10	10.10		
3+420.00	18.06	3+900.00	10.10		
3+440.00	18.43	3+901.02	10.09		
3+442.90	18.48	3+919.18	10.03		
3+460.00	18.73	3+920.00	10.03		
3+470.66	18.89	3+937.34	9.84		
3+480.00	19.07	3+940.00	9.82		
3+483.10	19.05	3+951.26	9.78		
3+500.00	18.99	3+960.00	9.80		
3+508.09	18.89	3+965.17	9.82		
3+520.00	19.04	3+966.11	9.83		
3+533.10	18.73	3+976.11	9.86		

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X.Θ.	Y	X.Θ.	Y	X.Θ.	Y
3+000.00	11.27	3+540.00	18.44	3+980.00	9.87
3+017.18	11.02	3+550.00	18.05	3+986.11	9.90
3+020.00	10.96	3+560.07	17.75	4+000.00	10.00
3+040.00	10.83	3+580.00	17.22		\$
3+042.19	10.83	3+587.04	17.09		
3+060.00	8.23	3+600.00	16.83		
3+067.18	8.20	3+612.05	16.55		
3+080.00	7.98	3+620.00	16.38		
3+100.00	7.80	3+637.04	15.90		
3+120.00	7.66	3+640.00	15.85		
3+140.00	7.60	3+648.39	15.71		
3+160.00	7.49	3+660.00	15.50		
3+180.00	7.50	3+680.00	15.14		
3+200.00	7.49	3+685.62	15.02		
3+220.00	8.19	3+700.00	14.72		
3+240.00	8.55	3+720.00	14.33		
3+243.08	8.63	3+722.85	14.27		
3+260.00	8.08	3+740.00	13.88		
3+270.84	8.68	3+747.42	13.71		
3+280.00	9.12	3+760.00	13.38		
3+298.64	10.21	3+771.98	13.03		
3+300.00	10.34	3+780.00	12.76		
3+313.75	12.40	3+800.00	11.98		
3+316.76	15.75	3+809.21	11.62		
3+320.00	15.71	3+820.00	11.26		
3+340.00	15.86	3+840.00	10.79		
3+356.87	16.26	3+846.44	10.63		
3+360.00	16.29	3+860.00	10.34		
3+380.00	16.96	3+873.19	10.11		
3+400.00	17.51	3+880.00	10.09		
3+415.11	17.93	3+887.10	10.10		
3+420.00	18.06	3+900.00	10.10		
3+440.00	18.43	3+901.02	10.09		
3+442.90	18.48	3+919.18	10.03		
3+460.00	18.73	3+920.00	10.03		
3+470.66	18.89	3+937.34	9.84		
3+480.00	19.07	3+940.00	9.82		
3+483.10	19.05	3+951.26	9.78		
3+500.00	18.99	3+960.00	9.80		
3+508.09	18.89	3+965.17	9.82		
3+520.00	19.04	3+966.11	9.83		
3+533.10	18.73	3+976.11	9.86		

X.Ø.	Y	X.Ø.	Y	X.Ø.	Y
0+000.00	148.15	0+599.77	145.13	1+220.30	145.97
0+016.97	148.16	0+619.47	145.14	1+238.36	146.19
0+033.95	148.17	0+639.05	145.17	1+257.45	146.41
0+047.80	148.18	0+657.43	145.24	1+275.48	146.62
0+061.65	148.19	0+676.91	145.27	1+295.31	146.81
0+080.28	148.20	0+685.21	145.30	1+314.02	147.00
0+099.09	148.21	0+688.58	145.32	1+333.63	147.05
0+101.90	148.24	0+691.95	145.34	1+352.73	147.16
0+108.79	148.26	0+709.78	145.43	1+356.78	147.20
0+115.67	148.24	0+727.39	145.45	1+363.78	147.27
0+134.93	148.16	0+730.33	145.44	1+370.77	147.35
0+153.44	148.10	0+733.27	145.45	1+390.02	147.65
0+173.26	148.02	0+752.32	145.43	1+408.13	148.09
0+188.65	147.97	0+771.31	145.30	1+427.36	148.77
0+198.29	147.94	0+789.85	145.04	1+446.43	149.57
0+207.93	147.91	0+792.34	145.02	1+456.37	149.96
0+227.34	147.94	0+811.03	144.93	1+467.06	150.28
0+245.47	148.02	0+827.31	144.93	1+477.55	150.59
0+263.73	148.03	0+845.42	144.91	1+489.16	150.80
0+282.31	148.06	0+862.27	144.94	1+498.72	150.93
0+301.23	147.67	0+882.23	145.07	1+518.58	150.84
0+314.92	147.24	0+901.02	145.12	1+537.54	150.84
0+317.70	147.16	0+919.91	145.20	1+557.25	150.77
0+320.48	147.08	0+939.49	145.31	1+571.28	150.87
0+338.67	146.55	0+958.37	145.41	1+585.31	150.92
0+357.12	146.34	0+967.76	145.46	1+604.19	151.37
0+375.53	146.21	0+973.52	145.50	1+623.66	152.10
0+395.16	146.07	0+979.28	145.53	1+641.82	152.69
0+413.67	145.99	0+998.63	145.71	1+646.36	152.79
0+432.06	145.81	1+018.31	146.10	1+661.85	153.14
0+437.40	145.75	1+036.70	146.45	1+677.33	153.27
0+443.72	145.69	1+039.72	146.51	1+695.92	153.11
0+450.03	145.65	1+052.57	146.64	1+715.13	152.96
0+469.86	145.46	1+063.46	146.63	1+733.71	153.04
0+488.66	145.41	1+076.03	146.37	1+752.77	153.14
0+506.79	145.33	1+087.21	146.18	1+771.90	153.28
0+525.72	145.22	1+106.41	145.90	1+790.80	153.54
0+544.30	145.18	1+125.91	145.67	1+809.22	154.02
0+563.71	145.13	1+144.97	145.51	1+828.00	154.74
0+583.33	145.04	1+163.20	145.48	1+846.25	155.34
0+592.46	145.09	1+182.50	145.62	1+865.36	155.93
0+596.12	145.12	1+201.13	145.75	1+883.39	156.17

X.Ø.	Y	X.Ø.	Y	X.Ø.	Y
1+895.59	156.08	2+627.22	136.24	3+231.29	145.37
1+907.23	155.88	2+639.35	136.46	3+249.61	145.79
1+919.21	155.54	2+648.03	136.64	3+266.18	146.32
1+931.07	155.01	2+666.14	136.75	3+281.06	146.71
1+950.34	154.03	2+685.23	136.95	3+293.60	147.00
1+969.73	153.07	2+705.06	137.16	3+307.97	147.26
1+989.19	152.06	2+724.94	137.36	3+321.03	147.56
2+005.74	151.15	2+733.87	137.45	3+335.19	147.88
2+024.86	150.06	2+747.00	137.57	3+351.87	148.23
2+043.84	149.09	2+748.89	137.58	3+359.58	148.36
2+063.29	148.24	2+763.92	137.67	3+371.56	148.55
2+081.95	147.28	2+783.79	137.82	3+391.31	148.91
2+100.81	146.26	2+803.60	138.01	3+407.93	149.02
2+120.73	145.23	2+816.44	138.11	3+421.41	149.15
2+139.43	144.17	2+826.54	138.19	3+433.33	149.21
2+155.92	143.28	2+842.66	138.34	3+448.02	149.27
2+173.58	142.27	2+862.04	138.57	3+462.71	149.32
2+178.89	141.99	2+873.13	138.72	3+478.67	149.36
2+182.03	141.80	2+884.21	138.87	3+493.57	149.44
2+195.37	141.15	2+901.16	139.07	3+500.71	149.45
2+208.13	140.50	2+909.01	139.22	3+507.85	149.46
2+224.85	139.61	2+915.03	139.23	3+524.06	149.49
2+239.11	138.83	2+921.04	139.24	3+538.19	149.51
2+253.36	138.10	2+921.08	139.30	3+542.48	149.50
2+272.86	137.14	2+939.36	139.63	3+546.77	149.50
2+291.29	136.12	2+959.35	140.01	3+566.68	149.61
2+309.68	135.19	2+978.03	140.37	3+584.79	149.59
2+328.10	134.39	2+979.77	140.42	3+603.92	149.62
2+347.77	134.13	2+986.33	140.54	3+623.66	149.63
2+366.00	134.11	2+992.89	140.65	3+642.22	149.58
2+384.52	134.22	3+012.06	140.94	3+649.14	149.68
2+403.28	134.27	3+024.77	141.06	3+662.49	150.08
2+421.06	134.30	3+028.35	141.16	3+675.83	150.37
2+440.38	134.32	3+038.44	141.45	3+695.32	150.83
2+457.61	134.37	3+052.11	141.67	3+698.46	150.92
2+475.74	134.48	3+071.30	142.02	3+701.61	151.05
2+494.18	134.67	3+090.76	142.38	3+721.01	151.70
2+513.37	134.88	3+110.61	142.74	3+739.83	152.43
2+526.99	135.06	3+130.02	143.07	3+757.85	153.14
2+538.50	135.22	3+149.27	143.45	3+777.39	154.03
2+548.80	135.33	3+168.00	143.87	3+783.98	154.30
2+560.23	135.46	3+187.38	144.33	3+795.40	154.73
2+570.62	135.59	3+205.45	144.74	3+806.61	155.09
2+588.74	135.77	3+208.42	144.81	3+818.77	155.61
2+608.52	135.92	3+211.39	144.88	3+829.25	155.86

X.Ø.	Y	X.Ø.	Y	X.Ø.	Y
3+848.04	156.31	4+447.40	165.93	4+608.22	156.00
3+867.09	156.63	4+459.45	166.00	4+617.99	155.00
3+886.92	156.83	4+464.05	165.00	4+621.86	154.64
3+905.96	157.11	4+464.45	165.00	4+627.82	154.00
3+924.34	157.35	4+464.55	165.00	4+627.86	154.00
3+942.40	157.69	4+466.45	165.00	4+628.33	154.00
3+945.78	157.75	4+466.95	165.00	4+641.45	153.00
3+948.62	157.81	4+466.96	165.00	4+641.77	153.00
3+951.46	157.87	4+467.51	165.00	4+642.24	153.00
3+969.92	158.21	4+471.50	165.00	4+643.14	153.00
3+989.42	158.62	4+483.88	164.00	4+654.48	153.00
4+008.40	159.01	4+483.91	164.00	4+663.83	152.00
4+027.77	159.50	4+484.36	164.00	4+664.41	152.00
4+031.28	159.60	4+492.04	163.82	4+678.44	151.23
4+035.13	159.70	4+498.20	163.00	4+679.98	151.00
4+038.96	159.81	4+498.41	163.00	4+687.96	150.84
4+058.69	160.34	4+498.62	163.00	4+695.97	150.00
4+078.28	160.88	4+500.15	162.94	4+697.48	149.97
4+096.37	161.37	4+508.25	162.89	4+699.05	150.00
4+100.74	161.49	4+519.89	162.00	4+699.07	150.00
4+105.10	161.58	4+519.94	162.00	4+699.12	150.00
4+123.58	161.93	4+520.06	162.00	4+699.57	150.00
4+142.62	162.21	4+520.38	162.00	4+699.87	150.00
4+161.46	162.76	4+520.40	162.00	4+700.10	150.00
4+179.48	163.10	4+520.68	162.00	4+705.36	149.00
4+198.37	163.45	4+521.00	162.00	4+719.58	148.00
4+202.37	163.75	4+530.12	161.00	4+719.76	148.00
4+213.30	164.10	4+531.50	161.00	4+720.16	148.00
4+224.22	164.20	4+532.30	161.00	4+721.16	148.00
4+244.07	164.60	4+539.35	160.82	4+721.19	148.00
4+263.32	164.94	4+554.01	160.49	4+738.87	147.00
4+265.01	165.00	4+559.05	161.00	4+740.24	146.91
4+273.08	166.05	4+565.00	161.00	4+747.58	146.85
4+281.14	165.25	4+565.04	161.00	4+753.86	146.00
4+299.46	165.50	4+568.67	161.49	4+754.00	146.00
4+317.73	165.67	4+572.42	162.00	4+754.40	146.00
4+337.61	165.85	4+581.09	162.00	4+754.92	145.93
4+357.38	166.06	4+589.79	161.00	4+769.44	145.00
4+376.19	166.27	4+596.47	160.00	4+774.45	144.74
4+378.99	166.29	4+597.99	159.00	4+786.44	144.00
4+392.65	166.36	4+597.99	159.00	4+789.34	143.77
4+406.31	166.41	4+600.38	158.00	4+803.64	142.90
4+424.69	166.35	4+600.56	158.00	4+818.99	141.78
4+443.58	166.01	4+600.62	158.00	4+832.83	140.71
4+446.18	166.00	4+604.43	157.00	4+851.72	139.47

X.Ø.	Y	X.Ø.	Y	X.Ø.	Y
4+871.62	138.18	5+420.10	107.44	6+030.61	75.93
4+890.32	137.00	5+431.44	106.73	6+049.89	75.33
4+909.97	135.82	5+442.77	106.02	6+069.04	74.71
4+920.11	135.34	5+458.34	105.09	6+086.97	74.08
4+930.26	134.86	5+476.95	103.87	6+092.93	73.88
4+946.83	134.30	5+496.53	102.68	6+098.90	73.70
4+949.59	134.20	5+515.17	101.45	6+117.00	73.13
4+964.17	133.68	5+533.58	100.40	6+136.92	72.53
4+977.81	133.23	5+552.17	99.17	6+156.88	71.98
4+992.74	132.70	5+571.13	97.89	6+176.62	71.44
5+006.03	132.26	5+590.71	96.70	6+195.32	70.97
5+025.99	131.59	5+605.86	95.72	6+212.24	70.56
5+045.40	130.97	5+617.41	95.02	6+220.47	70.34
5+063.55	130.31	5+628.96	94.31	6+228.69	70.11
5+065.93	130.25	5+647.76	93.15	6+246.79	69.61
5+071.74	129.94	5+653.25	92.82	6+266.20	69.03
5+076.01	129.76	5+666.74	91.92	6+285.58	68.53
5+086.09	129.23	5+685.43	90.61	6+304.85	68.11
5+104.22	127.99	5+703.93	89.24	6+324.70	67.68
5+120.30	127.01	5+723.20	88.03	6+333.66	67.49
5+125.46	126.69	5+743.15	86.86	6+337.45	67.43
5+130.62	126.38	5+763.08	85.71	6+341.23	67.37
5+150.36	125.12	5+769.61	85.32	6+360.26	67.01
5+169.60	123.88	5+776.71	84.88	6+378.04	66.69
5+188.21	122.71	5+783.81	84.45	6+381.60	66.62
5+206.52	121.52	5+803.40	83.31	6+385.17	66.54
5+225.77	120.28	5+822.97	82.34	6+404.04	66.18
5+227.33	120.19	5+827.93	82.11	6+423.56	65.75
5+234.19	119.74	5+830.24	82.03	6+442.19	65.37
5+241.06	119.28	5+832.56	81.88	6+461.01	65.04
5+260.67	117.89	5+850.96	81.25	6+479.18	64.71
5+279.19	116.64	5+867.06	80.66	6+497.73	64.30
5+286.60	116.14	5+873.14	80.55	6+516.36	63.78
5+292.57	115.73	5+879.22	80.36	6+518.71	63.73
5+298.28	115.42	5+898.58	79.89	6+521.05	63.67
5+303.40	115.12	5+916.78	79.48	6+540.28	63.20
5+307.96	114.88	5+924.28	79.26	6+560.01	62.71
5+312.51	114.59	5+931.66	79.03	6+565.41	62.64
5+331.46	113.40	5+939.04	78.78	6+570.58	62.58
5+351.20	112.11	5+957.16	78.19	6+575.74	62.48
5+369.03	110.91	5+977.02	77.66	6+594.07	62.02
5+379.62	110.19	5+996.26	77.02	6+610.80	61.61
5+390.21	109.48	6+005.43	76.73	6+616.57	61.45
5+402.80	108.59	6+008.27	76.63	6+622.35	61.29
5+411.45	108.03	6+011.10	76.53	6+641.73	60.88

X.Ø.	Y	X.Ø.	Y	X.Ø.	Y
6+661.48	60.51	7+384.11	51.34	8+109.64	48.56
6+679.97	60.15	7+402.96	51.14	8+123.85	48.70
6+686.37	59.99	7+422.54	50.94	8+142.01	48.91
6+692.16	59.84	7+441.04	50.75	8+161.75	49.10
6+697.96	59.70	7+459.32	50.44	8+181.69	49.11
6+717.49	59.18	7+477.75	49.83	8+199.72	49.12
6+736.00	58.85	7+496.83	49.52	8+203.74	49.12
6+754.65	58.56	7+515.71	49.15	8+218.29	49.22
6+773.59	58.29	7+534.46	48.79	8+232.85	48.97
6+791.94	58.00	7+553.46	48.41	8+251.05	48.39
6+810.07	57.80	7+571.68	48.13	8+270.34	47.58
6+829.20	57.60	7+582.78	47.97	8+274.70	47.41
6+848.48	57.42	7+593.35	47.81	8+282.05	47.11
6+850.87	57.41	7+603.93	47.63	8+289.40	46.77
6+869.69	57.34	7+622.96	47.28	8+308.36	46.09
6+888.52	57.29	7+641.20	47.01	8+327.76	45.42
6+908.17	57.11	7+660.59	46.80	8+347.27	44.75
6+927.15	56.94	7+679.42	46.58	8+367.26	44.07
6+945.84	56.77	7+697.83	46.34	8+367.36	44.06
6+962.73	56.58	7+716.69	46.08	8+386.41	43.53
6+973.90	56.42	7+735.14	45.92	8+405.45	42.80
6+985.08	56.20	7+753.30	45.75	8+425.01	41.84
6+998.64	55.81	7+772.30	45.61	8+444.75	40.97
7+015.40	55.35	7+781.11	45.53	8+464.45	40.23
7+030.02	55.04	7+790.16	45.43	8+482.45	39.65
7+047.06	54.87	7+799.20	45.39	8+502.06	39.06
7+061.41	54.73	7+817.21	45.41	8+505.70	38.96
7+080.41	54.56	7+837.01	45.42	8+520.26	38.59
7+098.69	54.32	7+843.91	45.33	8+534.35	38.19
7+118.41	54.18	7+863.25	45.34	8+548.99	37.93
7+135.68	54.07	7+883.22	45.37	8+562.99	37.59
7+155.30	53.98	7+899.46	45.48	8+581.62	37.35
7+172.66	53.84	7+919.23	45.57	8+600.76	37.30
7+191.58	53.60	7+938.37	45.74	8+613.21	37.31
7+211.02	53.31	7+954.99	45.94	8+627.21	37.26
7+230.34	53.09	7+973.19	46.12	8+640.04	36.98
7+249.02	52.88	7+993.07	46.29	8+653.50	36.35
7+263.49	52.73	8+011.89	46.64	8+666.87	35.88
7+272.28	52.68	8+025.47	46.90	8+685.46	35.36
7+281.07	52.62	8+030.42	47.01	8+704.54	35.05
7+301.02	52.41	8+035.37	47.12	8+724.19	34.80
7+319.61	52.14	8+053.96	47.46	8+742.94	34.61
7+338.72	51.87	8+073.02	47.86	8+761.25	34.49
7+354.39	51.68	8+092.49	48.24	8+779.98	34.30
7+369.25	51.50	8+095.43	48.32	8+799.05	34.16

X.Θ.	Y
8+818.39	34.10
8+829.08	34.09
8+846.08	34.21
8+863.08	34.48
8+876.33	34.66
8+891.97	34.82
8+907.61	35.39
8+927.46	36.14
8+946.76	36.70
8+949.60	36.76
8+952.44	36.82
8+972.18	37.19
8+990.74	37.14
8+994.99	37.13
\$	

X.Ø.	Y	X.Ø.	Y
0.00	109.46	2286.58	73.75
34.49	108.37	2334.13	71.46
73.14	107.32	2406.45	68.04
107.70	106.41	2462.76	65.69
139.28	105.75	2490.94	65.55
146.85	105.87	2146.21	75.04
155.54	105.83	2201.67	76.30
218.77	101.75	2286.58	73.75
261.14	100.69	2334.13	71.46
298.29	99.66	2406.45	68.04
353.89	97.79	2462.76	65.69
409.06	96.03	2490.94	65.55
472.00	94.47	2526.53	65.36
529.11	92.98	2615.90	64.67
571.32	91.97	2688.31	64.34
638.34	90.76	2740.38	64.58
705.88	89.67	2799.11	64.32
764.73	89.09	2855.20	64.30
803.22	88.73	2928.50	65.09
832.29	88.39	2992.88	66.64
865.95	88.19	3075.58	69.57
905.55	87.51	3136.97	71.20
945.59	87.03	3182.78	72.96
978.66	86.52	3235.37	74.53
1015.91	85.94	3302.68	77.80
1027.36	85.69	3371.40	82.14
1102.70	84.32	3432.53	84.58
1160.04	83.42	3481.38	86.53
1249.38	82.13	3556.78	88.49
1316.54	81.01	3613.87	92.84
1405.59	80.12	3660.37	95.86
1468.49	79.32	3683.61	96.95
1518.45	78.75	3713.16	97.86
1565.23	78.28	3760.22	98.84
1613.34	77.53	3808.53	99.41
1660.96	76.88	3882.95	101.86
1723.25	75.60	3939.51	105.43
1766.55	74.59	3984.95	109.20
1852.72	73.72	4014.80	110.11
1921.23	73.33	\$	
1997.16	73.35		
2085.57	73.78		
2146.21	75.04		
2201.67	76.30		

μ

Monte Carlo

```
import fdata
# import dxf
import repeat_xy
import geom

def pyMain():
    """Start here."""
    fn = "kalamata"
    fr = open(fn+".mhk", "r", encoding="iso-8859-7")
    amhk, xth, y, name = fdata.readData(fr)
    #fdata.plotmhk(amhk, xth, y, name)
    pl = fdata.PlotManyMhk()
    na = int((xth[-1] - xth[0])//500)
    ncarlo = 3
    for a in range(1, na+1):
        for i in range(ncarlo+1):
            print("Monte Carlo: nodes={}/{} try={}/{}".format(a, na, i,
ncarlo))
            po = repeat_xy.monteCarlo(xth, y, a)
            repeat_xy.saveCarlo(fn, po)
            # pl.plotmhk("MonteCarlo_nodes={}_area={:.1f}".format(po.a, po.emb),
xth, y, name, po.xers, po.yers)
            print(" Area: {:.2f} (geom={:.2f} overlapping={:.2f}
klish={:.2f})".format(po.emb, po.embGeom, po.embOverlapping, po.embKlish))
            s = geom.klisi(po.xers, po.yers)
            # fdata.showmhk(amhk, xth, y, name, po.xers, po.yers) #
                μ
            # for z in range(0, len(po.xers)-1, 2):
            #     x_cur = [a[0] for a in po.edafery()]
            #     y_cur = [a[2] for a in po.edafery()]
            #     fdata.show_curve(x_cur, y_cur)
            for slope in s:
                print(" Slope : {:.2f}%".format(slope*100))
            print(" main", po.yers, po.xers)
            # fdata.showend()
        # pl.plotend()
    fr.close()
```

pyMain()

fdata

```
import matplotlib.pyplot as plt
import numpy
import dxf
from scipy.interpolate import spline
```

```

def readData(f):
    "Read ground data from a file."
    #
    fxth = []
    fy = []
    fname = []
    iline = 0
    for amhk in f:
        iline += 1
        break
    for line in f:
        iline += 1
        if line.strip() == "$": break
        #   μ      string(line)
        #       μ              μ          μμ
        try:
            a, b, c = line.split()
            fxth.append(float(a))
            fy.append(float(b))
            fname.append(c)
        except (IndexError, ValueError):
            raise ValueError("Syntax error at line {} of file {}".format(iline,
f.name))
    return amhk, fxth, fy, fname

def writeRes(fw, xers, yers, emb):
    "Write the results to a file."
    fw.write("Area: {:.2f}\n".format(emb))
    fw.write("Grade points:\n")
    for x1, y1 in zip(xers, yers):
        fw.write("{:15.3f}{:15.3f}\n".format(x1, y1))
    fw.write("$\n")

def plotmhk(amhk, fxth, fy, fname, xers=(), yers=()):
    "Plots the profile in dxf format, both ground and grade line."
    dxf.plotstart()
    plotmhk1(amhk, fxth, fy, fname, xers, yers)
    dxf.plotend()

def plotmhk1(amhk, fxth, fy, fname, xers=(), yers=()):
    "Plots the profile in dxf format, both ground and grade line."
    dxf.plotsetlayer("EDAFOS")
    h = 10.0*10 #text size/height
    dxf.plotsymbol(fxth[0]-(len(amhk)+2)*h, fy[0]*10, h, amhk, 0.0)

    for m in range(1, len(fxth)):
        dxf.plotline(fxth[m - 1], fy[m - 1] * 10, fxth[m], fy[m] * 10)
        # plotline(fxth[m-1],fy[m-1]*10, fxth[m-1], min(fy)-)
        # plotsymbol(x1,y1,0.1,name[m-1],0)
    dxf.plotsetlayer("ERYTHRA")

```

```

for m in range(1, len(xers)):
    dxf.plotline(xers[m - 1], yers[m - 1] * 10, xers[m], yers[m] * 10)

class PlotManyMhk:
    "Call to plot multiple profiles to a single dxf."
    def __init__(self):
        "Open new drawing and set horizon."
        dxf.plotstart()
        self.hor = 0.0    #horizon (min of the profile on the drawing)

    def plotmhk(self, amhk, fxth, fy, fname, xers=(), yers=()):
        "Plots the profile in dxf format, both ground and grade line."
        temp = tuple(fy)+tuple(yers)
        fymin = min(temp)
        dy = max(temp) - fymin
        self.hor -= dy*1.1
        fyn = [self.hor+(temp-fymin) for temp in fy]
        yersn = [self.hor+temp-fymin for temp in yers]
        plotmhk1(amhk, fxth, fyn, fname, xers, yersn)

    def plotend(self):
        "Close the drawing."
        dxf.plotend()

def showmhk(amhk, fxth, fy, fname, xers=(), yers=()):
    "Plots the profile to a pyplot diagram."
    plt.figure(figsize=(1000, 1))
    plt.plot(fxth, fy, 'g-', xers, yers, 'b')
    # plt.axis('scaled')

def show_curve(x_c, y_c):
    # y = s1/100*x+x^2/(2*h)
    '''xnew = numpy.linspace(numpy.array(x_c).min(),numpy.array(x_c).max(),300)
    curve_smooth = spline(numpy.array(x_c),numpy.array(y_c),xnew)
    plt.plot(xnew, curve_smooth,'r--')'''
    plt.plot(x_c, y_c, 'r--')

def showend():
    plt.show()

repeat_xy

"""This module implements the Monte Carlo algorithm."""
import datetime
from pointcl import Point
import geom

```

```

import prodiagrafes
from math import fabs

ntriesperdim = 2000

def monteCarlo(xth, y, a):
    """Using Monte Carlo find optimum grade points."""
    Point.setGround(xth, y)
    po = Point(a)
    pomin = Point(a)
    ntries = a*2 * ntriesperdim

    for itry in range(ntries):
        if itry>0 and itry %1000 == 0:
            print("      {}/{}".format(itry, ntries))
        for iover in range(3): #Make at most 3 tries if overlapping happens
            po.setRandomErs()
            po.computeGeom()
            if po.embOverlapping == 0.0: break
        if po.emb < pomin.emb:
            pomin, po = po, pomin
    return pomin

def saveCarlo(fn, po):
    "Append the results of a Monte-Carlo run to a file."
    d = datetime.datetime.today()
    with open(fn+".car", "a", encoding="iso-8859-7") as fw: # open the file for
append
        fw.write("#Monte Carlo: nodes={:<3d}  carlotries={:<5d}
{}}\n".format(po.a,
                ntriesperdim, d.isoformat(" ")))
        fw.write("#          Area={:<10.3f}  (geom={:<10.3f}
overlapping={:<10.3f}  klish={:<10.3f})\n".format(po.emb, po.embGeom,
po.embOverlapping, po.embKlish))
        fw.write("{:.2f}\n".format(po.emb))
        fw.write("{:d}\n".format(len(po.xers)))
        r = list(po.h)
        r.insert(0, 0.0)
        r.append(0.0)
        for i in range(len(po.xers)):
            fw.write("{:15.3f}{:15.3f}{:15.3f}\n".format(po.xers[i], po.yers[i],
r[i]))
        fw.write("\n") #blank line

```

pointcl

```

import random
import prodiagrafes

```

```

import parametroi_kampilis
from geom import plinint, klisi, d_klisi, proarea, elegxos_s
from math import fabs

class Point:
    """Computes random grade points, the elevation of the grade points
    and the area between grade and ground line."""
    ve, s_max, hk, hw = prodiagrafes.vasikes_parametroi()
    embmax = 1.0e100

    @classmethod
    def setGround(cls, xth, y):
        "Set the ground and number of nodes for all objects in this class."
        cls.xth = tuple(xth)
        cls.y = tuple(y)

    def __init__(self, a, xers=None, yers=None):
        "Set the geometry of the profile; compute random nodes if needed."
        self.a = a
        if xers is None:
            self.setRandomErs()
        else:
            assert len(self.xers) == a+2
            self.xers = list(xers)
            self.yers = list(yers)
            self.computeGeom()

    def computeGeom(self):
        "(Re)compute geometry of the profile."
        self.s = klisi(self.xers, self.yers)
        self.ds = d_klisi(self.xers, self.yers)
        self.h = parametroi_kampilis.dtrmn_h(Point.hw, Point.hk, self.s)
        self.t = parametroi_kampilis.dis_t(self.h, self.ds)
        self.embOverlapping = self.penaltyOverlapping()
#Additional area (penalty) due to overlapping
        self.embKlish = fabs(elegxos_s(self.xers, self.yers, Point.s_max))
#Additional area (penalty) due to excess slope
        self.embGeom = proarea(self.edafery()) #Area
of profile
        self.emb = self.embGeom + self.embOverlapping + self.embKlish

    def setRandomErs(self):
        "(Re)set random nodes."
        xers = []
        xers.append(self.xth[0])
        xers.append(self.xth[-1])
        for i in range(self.a): # a is the number of grade points between the
first and last station
            xers.append(random.uniform(xers[0], xers[1]))
        xers.sort()
        self.xers = xers

```

```

        self.yers = Point.random_yers(self.xers, self.xth, self.y)

    @staticmethod
    def random_yers(xers, xth, y):
        """Computes the elevation of the grade points: ground elevation +-30
m."""
        yers = []
        yers.append(y[0])
        for i in range(1, (len(xers)-1)):
            yers.append(plinint(xth, y, xers[i])+random.uniform(-30.0, 30.0))
        yers.append(y[-1])
        return yers

    def penaltyOverlapping(self):
        "Penalty due to overlapping of two consecutive vertical curves."
        penalty = 0.0
        for e in range(1, len(self.t)):
            tt = fabs(self.t[e]) + fabs(self.t[e-1])
            xx = self.xers[e] - self.xers[e-1]
            if tt > xx:
                penalty += (tt-xx)*30.0
        return penalty

    def edafery(self):
        """Computes the grade line for all ground points and the ground line for
all grade points."""
        xeds2 = self.xth
        yeds2 = self.y
        xarx = xeds2[0]
        xtcl = xeds2[-1]
        basic_x = parametroi_kampilis.curve(self.xers, self.ds, self.h) #Start
x and end x of all curves
        cc3 = [(b_x, plinint(xeds2, yeds2, b_x), plinint(self.xers, self.yers,
b_x)) for b_x in basic_x
                if xarx<b_x<xtcl] #If we have overlapping, basic_x may be out
of the profile
        cc1 = [(xer, plinint(xeds2, yeds2, xer),
                parametroi_kampilis.in_out_curve(self.xers, self.yers, xer,
self.ds, self.h))
                for (xer, yer) in zip(self.xers, self.yers)]
        cc2 = [(xed, yed, parametroi_kampilis.in_out_curve(self.xers, self.yers,
xed, self.ds, self.h)) for (xed, yed) in zip(xeds2, yeds2)]
        cc2.extend(cc1)
        cc2.extend(cc3)
        cc2.sort()
        return cc2

```


geom

```
"""This modules defines geometry functions."""
from math import fabs

def plinint(xers, yers, x):
    "Interpolates x in polyline defined by xers, yers."
    if x < xers[0] or x > xers[-1]:raise ValueError("Out of range")
    for i in range(1, len(xers)):
        if x <= xers[i]:
            return linint(xers[i-1], yers[i-1], xers[i], yers[i], x)

def linint(x1, y1, x2, y2, x):
    "Linear interpolation without checking for zero denominator."
    return y1 + (y2-y1)/(x2-x1) * (x-x1)

def d_klisi(xers, yers):
    return [j-i for i, j in zip(klisi(xers, yers)[: -1], klisi(xers, yers)[1:])]

def klisi(xers, yers):
    return [(yers[i]-yers[i-1])/(xers[i]-xers[i-1]) for i in range(1, len(xers))]

def proarea(cc):
    """Computes the positive and negative areas between grade and ground line."""
    def area(x1, dy1, x2, dy2):
        """Computes area between two points and adds it to positive or negative
sums."""
        nonlocal epos, eneg
        e = (dy1+dy2) * (x2-x1) / 2
        if e > 0: epos += e
        else: eneg += e

    epos = eneg = 0.0
    x = [ca[0] for ca in cc]
    dy = [ca[1]-ca[2] for ca in cc]
    for i in range(len(x)-1):
        j = i + 1
        if dy[i]*dy[j] >= 0:
            area(x[i], dy[i], x[j], dy[j])
        else:
            xm = linint(dy[i], x[i], dy[j], x[j], 0.0)
            area(x[i], dy[i], xm, 0.0)
```

```

        area(xm, 0.0, x[j], dy[j])
    return epos-eneg

```

```

def elegxos_s(xers, yers, s_max):
    "Additional penalty (area units) in case some slope exceeds max slope."
    kl = klisi(xers, yers)
    eplus = 0.0
    for i in range(1, len(xers)):
        ak1 = fabs(kl[i-1])
        if ak1 > s_max:
            eplus += 30.0*(xers[i]-xers[i-1]) * fabs(ak1-s_max)/s_max
    return eplus

```

prodiagrafes

```

def vasikes_parametroi():
    ve_d = [ 50, 60, 70, 80, 90, 100, 110, 120, 130]
    hk_d = [-1400, -3000, -4500, -6200, -8000, -10000, -15000, -15000, -15000]
    #Crest vertical curve radius OMOE-X teyxos 3 8/6/2001
    hw_d = [ 1350, 1900, 2500, 3300, 4200, 5200, 6300, 7500, 10000] #Sag
    vertical curve radius
    global ve, s_max, hk, hw
    ve = 70 # μ
    kat_odou = "A"
    kat_ed = " "
    if kat_odou == "A":
        s_max = katigoria_a(ve, ve_d, kat_odou, kat_ed)
    elif kat_odou == "B" :
        s_d = [0.08, 0.07, 0.06, 0.05]
        s_max = s_d[ve_d.index(ve)]
    else:
        raise ValueError("Wrong road type")
    hk = hk_d[ve_d.index(ve)]
    hw = hw_d[ve_d.index(ve)]

    return ve, s_max, hk, hw

```

```

def katigoria_a(ve, ve_d, kat_odou, kat_ed):
    """Computes maximum grade."""
    if kat_ed == " ":
        s_d = [0.07, 0.06, 0.05, 0.04, 0.04, 0.03, 0.03, 0.03, 0.03]
    elif kat_ed == " ":
        s_d = [0.08, 0.07, 0.06, 0.05, 0.05, 0.04, 0.04, 0.04]
    elif kat_ed == " ":
        s_d = [0.10, 0.09, 0.08, 0.07, 0.07, 0.06, 0.05]
    else:
        raise ValueError("Wrong terrain type")
    s = s_d[ve_d.index(ve)] #This may raise IndexError
    return s

```

parametroi_kampilis

```
import geom

def dtrmn_h(hw, hk, s): # xers list has two more elements than h
    """Finds a list about radius h between two lines"""
    h = []
    for i in range(1, len(s)):
        if s[i] < s[i-1]: h.append(hk) #sag
        else: h.append(hw) #crest
    return h

def dis_t(h, ds): # t list has as much elements as xers list. The first and the
last is 0
    """Finds a list about distance t in vertical curve"""
    t = list(map(lambda x, y: (x*y)/2, h, ds))
    t.append(0.0)
    t.insert(0, 0.0)
    return t

def curve(xers, ds, h):
    """Estimates the first and the last x coordinate of a vertical curve"""
    basic_x = [xers[i] - dis_t(h, ds)[i] for i in range(1, len(xers)-1)]
    basicx_1 = [xers[i] + dis_t(h, ds)[i] for i in range(1, len(xers)-1)]
    basic_x.extend(basicx_1)
    basic_x.sort()
    return basic_x

def in_out_curve(xers, yers, x, ds, h):
    d_t = dis_t(h, ds)
    # print("parametroi kampilis inout", d_t)
    if x < xers[0] or x > xers[-1]: raise ValueError("Out of range")
    for e in range(1, len(xers)-1):
        if x>=xers[e]-d_t[e] and x<=xers[e]: return alt_curve_x(xers, yers, x,
d_t, h, e)
        elif x>xers[e] and x<=xers[e]+d_t[e]: return alt_curve_x_plus(xers, yers,
x, d_t, h, e)
    else: return geom.plinint(xers, yers, x)

def alt_curve_x(xers, yers, x, d_t, h, e):
    """Estimates the altitude of a point in a vertical curve"""
    alt = geom.linint(xers[e-1], yers[e-1], xers[e], yers[e], x)+((x-(xers[e]-
d_t[e]))**2/(2*h[e-1]))
    return alt

def alt_curve_x_plus(xers, yers, x, d_t, h, e):
```

```

    """Estimates the altitude of a point in a vertical curve"""
    alt = geom.linint(xers[e], yers[e], xers[e+1], yers[e+1], x)+((x-
(xers[e]+d_t[e]))**2/(2*h[e-1]))
    return alt

    dxf

out = None
lay = "0" #default layer

def plotstart():
    global out
    out = open("data5.dxf", "w")
    for line in "0 SECTION 2 HEADER 9 ACADVER 1 $AC1009 0 ENDSEC 0 SECTION 2
ENTITIES".split():
        out.write(line+"\n")

def plotline(x1, y1, x2, y2):
    plot = "0 LINE 8 {0} 10 {1} 20 {2} 11 {3} 21 {4}".format(lay, x1, y1, x2, y2)
    for line in plot.split():
        out.write(line+"\n")

def plotend():
    for line in "0 ENDSEC 0 EOF".split():
        out.write(line+"\n")
    out.close()

def plotsymbol(x1, y1, h, txt, theta):
    ps = "0 TEXT 8 {0} 10 {1} 20 {2} 40 {3} 1 {4} 50 {5}".format(lay, x1, y1, h,
txt, theta)
    for line in ps.split():
        out.write(line+"\n")

def plotsetlayer(laynew):
    "Set layer for all following objects."
    global lay
    lay = laynew

```

Multiprocessing

```
import multiprocessing
import fdata
import repeat_xy
import korerythras
import geom
from pointcl import Point

def monteCarlo(xth, y, a): # comment for linux
    """Using Monte Carlo find optimum grade points."""
    Point.setGround(xth, y)
    ntries = a*2 * repeat_xy.ntriesperdim
    pomin = Point(a)

    nprocesses = multiprocessing.cpu_count()
    ntries1 = ntries//nprocesses
    pool = multiprocessing.Pool(nprocesses)

    argslst = [(a, ntries1)] * nprocesses
    for pol in pool.imap_unordered(repeat_xy.doSome, argslst):
        if pol.emb < pomin.emb:
            pomin = pol
    return pomin

def pyMain():
    """Start here."""
    fn = "road_name"
    fr = open(fn+".mhk", "r", encoding="iso-8859-7")
    amhk, xth, y, name = fdata.readData(fr)
    #fdata.plotmhk(amhk, xth, y, name)
    pl = fdata.PlotManyMhk()
    na = int((xth[-1] - xth[0])//500)
    ncarlo = 38

    for a in range(1, na+1):

        Point.setGround(xth, y)
        ntries = a*2 * repeat_xy.ntriesperdim
        pomin = Point(a)

        if __name__ == '__main__': # comment for linux
            nprocesses = multiprocessing.cpu_count()
            ntries1 = ntries//nprocesses
            pool = multiprocessing.Pool(nprocesses)

            argslst = [(a, ntries1)] * nprocesses
            for pol in pool.imap_unordered(repeat_xy.doSome, argslst):
```

```

        if pol.emb < pomin.emb:
            pomin = pol

    for i in range(1, ncarlo+1):
        print("Monte Carlo: nodes={}/{}    try={}/{}".format(a, na, i,
ncarlo))

        # po = repeat_xy.monteCarlo(xth, y, a) # uncomment for linux
        po = monteCarlo(xth, y, a)
        repeat_xy.saveCarlo(fn, po)
        pl.plotmhk("MonteCarlo_nodes={}_area={:.1f}".format(po.a,
po.emb), xth, y, name, po.xers, po.yers)
        print("    Area: {:.2f} (geom={:.2f} overlapping={:.2f}
klish={:.2f})".format(po.emb, po.embGeom, po.embOverlapping, po.embKlish))
        s = geom.klisi(po.xers, po.yers)
        # fdata.showmhk(amhk, xth, y, name, xers, yers)
        # for z in range(0, len(xers)-1, 2):
        #     x_cur = [a[0] for a in korerythras.edafery(xers, yers, xth,
y)]
        #     y_cur = [a[2] for a in korerythras.edafery(xers, yers, xth,
y)]

        #     fdata.show_curve(x_cur, y_cur)
        for slope in s:
            print("    Slope : {:.2f}%".format(slope*100))
        print("    main", po.yers, po.xers)
        # fdata.showend()

    pl.plotend()
    fr.close()

```

```
pyMain()
```

```
repeat_xy
```

```
"""This module implements the Monte Carlo algorithm."""
```

```
import datetime
from pointcl import Point
import geom
import prodiagrafes
from math import fabs
import multiprocessing
```

```
ntriesperdim = 2000
```

```

# def monteCarlo(xth, y, a):
#     """Using Monte Carlo find optimum grade points."""
#     Point.setGround(xth, y)
#     ntries = a*2 * ntriesperdim
#     pomin = Point(a)
#
#     if __name__ == '__main__':

```

```

#         nprocesses = multiprocessing.cpu_count()
#         ntries1 = ntries//nprocesses
#         pool = multiprocessing.Pool(nprocesses)
#
#         argslst = [(a, ntries1)] * nprocesses
#         for pol in pool.imap_unordered(doSome, argslst):
#             if pol.emb < pomin.emb:
#                 pomin = pol
#         return pomin

def monteCarloSingle(xth, y, a):
    """Using Monte Carlo find optimum grade points; using a single cpu/core."""
    Point.setGround(xth, y)
    ntries = a*2 * ntriesperdim

    pomin = doSome((a, ntries))
    return pomin

def doSome(args):
    "Do some of the iterations."
    a, ntries = args
    po = Point(a)
    pomin = Point(a)
    for itry in range(ntries):
        if itry>0 and itry %1000 == 0:
            print("      {}/{}".format(itry, ntries))
        for iover in range(3): #Make at most 3 tries if overlapping happens
            po.setRandomErs()
            po.computeGeom()
            if po.embOverlapping == 0.0: break
        if po.emb < pomin.emb:
            pomin, po = po, pomin
    return pomin

def saveCarlo(fn, po):
    "Append the results of a Monte-Carlo run to a file."
    d = datetime.datetime.today()
    with open(fn+".car", "a", encoding="iso-8859-7") as fw: # open the file for
append
        fw.write("#Monte Carlo: nodes={:<3d}  carlotries={:<5d}
{}}\n".format(po.a,
                ntriesperdim, d.isoformat(" ")))
        fw.write("#          Area={:<10.3f}  (geom={:<10.3f}
overlapping={:<10.3f}  klish={:<10.3f})\n".format(po.emb, po.embGeom,
po.embOverlapping, po.embKlish))
        fw.write("{:.2f}\n".format(po.emb))
        fw.write("{:d}\n".format(len(po.xers)))
        r = list(po.h)
        r.insert(0, 0.0)

```

```

        r.append(0.0)
    for i in range(len(po.xers)):
        fw.write("{:15.3f}{:15.3f}{:15.3f}\n".format(po.xers[i], po.yers[i],
r[i]))
    fw.write("\n")    #blank line

```

μ

```

import datetime
import geom
import fdata
from genal import GeneticAnimal, GeneticAlgorithm
from pointcl import Point
import genal

class PointAnimal(GeneticAnimal):

    def crhom2Fenotype(self, ga):
        """Transfer the instructions in chromosomes to the physical nature of the
animal."""
        a = ga.comNchrom
        xtha = Point.xth[0]
        xtht = Point.xth[-1]
        dx = (xtht - xtha)/ga.comNvalmax
        xers = [xtha]
        for i in range(a):
            xers.append(xtha + dx*self.chrom[i])
        xers.append(xtht)
        xers.sort()
        self.po = Point(a, xers)

    def justFitness(self, ga):
        """The fitness of the animal; the bigger the better."""
        return self.po.emb

def prg(fr, tags=()):
    "Print converting to DOS greek only if we run windows (tags is for
compatibility)."
    print(fr)

def pyMain():
    """Start here."""
    fn = "art1"
    fr = open(fn+".mhk", "r", encoding="iso-8859-7")
    amhk, xth, y, name = fdata.readData(fr)
    pl = fdata.PlotManyMhk()

```



```

Point.setGround(xth, y)

na = int((xth[-1] - xth[0])//500)
ncarlo = 3
ga = GeneticAlgorithm(prt=prg, nValmax=16384, nChrom=1, fitmax=30.0*(xth[-1]-
xth[0]), biggerIsBetter=False)
for j in range(2, na + 1, 2):
    for a in range(j, j + 1):
        for i in range(1, ncarlo+1):
            print("Genetic: nodes={}/{} try={}/{}".format(a, na, i,
ncarlo))
            ga = GeneticAlgorithm(prt=prg, nValmax=16384, nChrom=a,
fitmax=30.0*(xth[-1]-xth[0]), biggerIsBetter=False)
            ga.config(pmut = ga.pmut/5.0) #1 mutation every 5 generations

            ga.genetic(PointAnimal)
            po = ga.bestall.po
            saveGenetic(fn, po)
            pl.plotmhk("Genetic_nodes={}_area={:.1f}".format(po.a, po.emb),
xth, y, name, xth, [c[2] for c in po.edafery()]) #po.xers, po.yers)
            print("    Area: {:.2f} (geom={:.2f} overlapping={:.2f}
klish={:.2f})".format(po.emb, po.embGeom, po.embOverlapping, po.embKlish))
            s = geom.klisi(po.xers, po.yers)
            # fdata.showmhk(amhk, xth, y, name, xers, yers)
            # for z in range(0, len(xers)-1, 2):
            #     x_cur = [a[0] for a in korerythras.edafery(xers, yers, xth,
y)]
            #     y_cur = [a[2] for a in korerythras.edafery(xers, yers, xth,
y)]

            #     fdata.show_curve(x_cur, y_cur)
            for slope in s:
                print("    Slope : {:.2f}%".format(slope*100))
            print("    main", po.yers, po.xers)
            # fdata.showend()

pl.plotend()
fr.close()

def saveGenetic(fn, po):
    "Append the results of a Monte-Carlo run to a file."
    d = datetime.datetime.today()
    with open(fn+".car", "a", encoding="iso-8859-7") as fw: # open the file for
append
        fw.write("#Genetic alg: nodes={:<3d}   {}\n".format(po.a, d.isoformat("
"))))
        fw.write("#                Area={:<10.3f} (geom={:<10.3f}
overlapping={:<10.3f} klish={:<10.3f})\n".format(po.emb, po.embGeom,
po.embOverlapping, po.embKlish))
        fw.write("{:.2f}\n".format(po.emb))
        fw.write("{:d}\n".format(len(po.xers)))
        r = list(po.h)
        r.insert(0, 0.0)
        r.append(0.0)

```

```

        for i in range(len(po.xers)):
            fw.write("{:15.3f}{:15.3f}{:15.3f}\n".format(po.xers[i], po.yers[i],
r[i]))
        fw.write("\n")    #blank line

```

```

pyMain()

```

genal

```

from math import log2, fabs
import random
import copy

```

```

def prg(fr, tags=()):
    "Print converting to DOS greek only if we run windows (tags is for
compatibility)."
    print(fr)

```

```

class GeneticAlgorithm(object):

```

```

    """The class implements the genetic algorithm for optimisation."""

```

```

    def __init__(self, *args, **kw):

```

```

        # stin arxi eixe **kw egw to ekana *args kai sti seira 45

```

```

        """Initialize genetic algorithm procedure.

```

```

        These values are typical. They will be overwritten by genetic()."""

```

```

        self.prt = prg

```

```

        self.nAnim = None        # (initial?) number of animals

```

```

        self.animals = set()     # set of all animals alive

```

```

        self.bests = []         # Best animal of each generation

```

```

        self.bestall = None     # Best animal of all

```

```

        self.nGen = 200         # Number of generations

```

```

        self.igen = 0          # Current generation

```

```

        self.pmut = 0.0        # probability of mutation (if not set by user,

```

```

once every generation)

```

```

        self.r = random.Random()

```

```

        self.nRuns = 1         # Number of runs that the algorithm will be
executed

```

```

        self.comNvalmax = 2     # Integer max value (0..value-1) that a
chromosome may have (usually 2)

```

```

        self.comNchrom = 26    # Number of (different) chromosomes

```

```

        self.comFitmax = 0.0    # A big fitness; in fact it should be the best
fitness (biggest) possible (if known)

```

```

                                     # It is used to compute deficiency due to common
chromosomes between parents.

```

```

# If comBiggerIsBetter is False, comFitamx should
again be a big value (poor):
# it is used convert small values (which are
better) to big values (which the GA
# tries to maximise).
# If zer0, then the biggest fitness of all
animals (which are random) at the beginning is taken
self.nSample = 10 # Number animals taken is sample in
tournamentThanasis(); the least fit of these animals dies.
self.comBiggerIsBetter = True # If true justFitness() returns a number
which must be maximised
# If false justFitness() returns a
number which must be minimised
self.config(*args, **kw)

def config(self, prt=None, nAnim=None, nGen=None, pmut=None, nValmax=None,
nChrom=None, fitmax=None, biggerIsBetter=None):
    """Change default values."""
    if prt is not None: self.prt = prt
    if nAnim is not None:
        if nAnim < self.nSample: raise ValueError("At least %d animals are
required (for tournamentThanasis())" % (self.nSample,))
        self.nAnim = nAnim
    if nGen is not None: self.nGen = nGen
    if pmut is not None: self.pmut = pmut
    if nValmax is not None: self.comNvalmax = nValmax
    if nChrom is not None: self.comNchrom = nChrom
    if fitmax is not None: self.comFitmax= fitmax
    if biggerIsBetter is not None: self.comBiggerIsBetter = biggerIsBetter
    if self.nAnim is None: # If bo value, compute it
        self.nAnimCompute()
    elif nAnim is None: # If nAnim is not None, then the user wants
nAnim (which is already set)
        if nValmax is not None or nChrom is not None: # If nValmax and
nChrom are both None, there is nothing new to compute
            self.nAnimCompute()
    if self.pmut <= 0.0:
        self.pmutCompute()
    elif nAnim is not None: # If the number of animals changes, the
probability must change
        self.pmutCompute()

def nAnimCompute(self):
    """Compute the number of animals from other values (and change the value
of mutation probability).

    According to tournamentThanasis() we choose a random set of nSample (10)
animals
delete the one with the lowest fitness, until 50% of animals are deleted.
Thus we must have at least 2*nSample (20) animals, so that when we delete
half of them,
we still have nSample (10) animals to choose a random set."""
    self.nAnim = int(5 * log2(self.comNvalmax) * self.comNchrom) # 5

```

```

animals per binary chromosome
    self.nAnim = max(self.nAnim, 2*self.nSample) # At least 2*nSample (20)
animals anyway
    self.pmutCompute()

def pmutCompute(self):
    """Compute the probability of mutations: once per generation.

    According to tournamentThanasis() and breed(), the whole population
    of animals is replaced in every generation. 50% of the population dies.
    The remaining 50% are going to be parents. However only the parents get
    mutations. Thus nAnim/2 animals may mutate in each generation."""
    self.pmut = 1.0 / (self.nAnim/2.0)

def fitmaxCompute(self, DisAnimal):
    """Compute a big fitness; in fact it should be the best fitness possible.

    At the beginninbgt the animals are random. Thus the biggest fitness of
    all animals is
    a reasonable big fitness.
    """
    self.comFitmax = max(anim.justFitness(self) for anim in self.animals)

def genetic(self, DisAnimal):
    "Execute the genetic algorithm."
    self.animals.clear()
    del self.bests[:]
    for i in range(self.nAnim):
        self.animals.add(DisAnimal(self))
    if self.comFitmax == 0: self.fitmaxCompute(DisAnimal)
    for self.bestall in self.animals: break # Give a initial value to
bestall
    for self.igen in range(self.nGen):
        # print "Generation%4d" % igen
        self.bestIngen(self.igen)
        if self.converged(): break
        self.tournamentthanasis()
        self.breed()
    else:
        self.bestIngen(self.nGen)
        self.prt("Genetic algorithm terminated due to max generations",
"can1")
        # self.prt("\nBest fitness for every generation", "info1")
        # for i,b in enumerate(self.bests):
        #     self.prt("%4d: %.2f(%.2f)" % (i, b.fitness(self), b.fitnessr(self)))
        self.prt("")
        self.prt("best of all:", "info")
        if self.comBiggerIsBetter:
            self.prt("%.2f(%.2f)" % (self.bestall.fitness(self),
self.bestall.fitnessr(self)))
        else:
            self.prt("%.2f(%.2f)" % (self.comFitmax-self.bestall.fitness(self),
self.comFitmax-self.bestall.fitnessr(self)))

```

```

def converged(self):
    "Check if the genetic algorithm converged; 20 steps with no optimisation."
    if len(self.bests) < 100: return False    # At least 100 generations
    nc = 30
    if len(self.bests) < nc: return False
    flast = self.bests[-1].fitnessr(self)
    for anim in self.bests[-nc:]:
        f = anim.fitnessr(self)
        if thanNearx(f, flast): continue # flast is equal to f
        if flast > f: return False        # flast is a better value than f;
not converged
    return True

def bestIngen(self, igen):
    """Find and save the best animal in generation igen."""
#    print "-----"
    ---"
    best = max(self.animals, key=lambda a:a.fitnessr(self))
    if self.comBiggerIsBetter:
        self.prt("generation%4d best: %.2f(%.2f)" % (igen,
best.fitness(self), best.fitnessr(self)))
    else:
        self.prt("generation%4d best: %.2f(%.2f)" % (igen, self.comFitmax-
best.fitness(self), self.comFitmax-best.fitnessr(self)))
    self.bests.append(best)

def breed(self):
    """Animals mate and give birth to children."""
    anims = set()
    while len(self.animals) > 1:
        a, b = self.r.sample(self.animals, 2)
        self.animals.remove(a)
        self.animals.remove(b)
        a.mutate(self)
        b.mutate(self)
        for i in range(4):
            ch = a.mate(self, b)
            anims.add(ch)
    anims.update(self.animals)
    self.animals = anims

def tournamentclassic(self):
    "Select the best part of the population to breed; allow for a bit random
selection."
    pdie = 0.30
    nkeep = int(self.nAnim*(1-pdie))
    keep = set()
    for i in range(nkeep):
        pop = self.r.sample(self.animals, 4)
        a = max(pop, key=lambda a:a.fitness(self))
        keep.add(a)
        self.animals.remove(a)

```

```

        f = a.fitness(self)
#         print "%f -> %f -> %.1f      μ          " % (f, com.fitmax,
f/fa*100.0)
        for a in self.animals:
            f = a.fitness(self)
#         print "%f -> %f -> %.1f          " % (f, com.fitmax, f/fa*100.0)

    def tournamentthanasisis(self):
        """Select the best part of the population to breed; allow for a bit
random selection."""
        pdie = 0.50
        ndie = int(self.nAnim*pdie)
        for i in range(ndie):
            pop = self.r.sample(self.animals, self.nSample)
            a = min(pop, key=lambda a:a.fitness(self))
            self.animals.remove(a)
#         print "%.2f(%.2f) <= %.2f          " % (a.fitness(), a.fitnessr(),
com.fitmax)
#         for a in self.animals:
#             print("%.2f(%.2f) <= %.2f      " % (a.fitness(), a.fitnessr(),
com.fitmax))

class GeneticAnimal(object):
    """An animal representing the problem to optimise."""
    comR = random.Random()

    def __init__(self, ga, chrom1=None, deficiency=0.0):
        """Create chromosomes for the distribution animal."""
        if chrom1 == None:
            self.chrom = [0]*ga.comNchrom
            for i in range(ga.comNchrom): self.chrom[i] =
self.comR.randrange(ga.comNvalmax)
        else:
            assert len(chrom1) == ga.comNchrom
            self.chrom = list(chrom1)
        self.chrom.sort()          #2018_09_30
        self.crhom2Fenotype(ga)
        self.defic = deficiency          # Deficiency due to degeneration
        self.ftns = None

    def crhom2Fenotype(self, ga):
        """Transfer the instructions in chromosomes to the physical nature of the
animal."""
        pass

    def mutate(self, ga):
        """Perform a random mutation."""
        r = self.comR
        if r.random() > ga.pmut: return          #Mutate 1 in 1000 (look com.py)
        old = self.fitness(ga)
        oldr = self.fitnessr(ga)
        n = len(self.chrom)

```

```

if r.random() < -1.0: #2018_09_30
    i1 = r.randrange(n)
    monkey1 = self.chrom[i1]
    for i in range(10):
        i2 = r.randrange(n)
        monkey2 = self.chrom[i2]
        if monkey1 != monkey2: break
    else:
        ga.prt("Warning: can't find 2 chromosomes with different values",
"can1")
        return
    self.chrom[i1] = monkey2
    self.chrom[i2] = monkey1
else:
    i1 = r.randrange(n)
    monkey1 = self.chrom[i1]
    for i in range(10):
        monkey2 = r.randrange(ga.comNvalmax)
        if monkey1 != monkey2: break
    else:
        ga.prt("Warning: can't find different value to assign to
chromosome", "can1")
        return
    self.chrom[i1] = monkey2
self.chrom.sort() #2018_09_30
self.crhom2Fenotype(ga)
self.ftns = None
self.defic = 0.0
if ga.comBiggerIsBetter:
    ga.prt("          mutation: %.2f(%.2f) -> %.2f(%.2f)" % (old, oldr,
self.fitness(ga), self.fitnessr(ga)), "info1")
else:
    ga.prt("          mutation: %.2f(%.2f) -> %.2f(%.2f)" %
(ga.comFitmax-old, ga.comFitmax-oldr, ga.comFitmax-self.fitness(ga),
ga.comFitmax-self.fitnessr(self)), "info1")

def mate2(self, other):
    """Make 2 children which replace the parents, with change of a sequence
of chromosomes."""
    r = self.comR
    if r.random() < 0.7: return # 30% of the parents do not mate
    n = len(self.ban)
    n2 = int(n//2)
    i1 = r.randrange(n2)
    i2 = r.randrange(n2, n+1)
    self.chrom[i1:i2], other.chrom[i1:i2] = other.chrom[i1:i2],
self.chrom[i1:i2]
    self.ftns = None
    other.ftns = None

def mate(self, ga, other):
    """Make 1 children with mixed chromosomes of the parents."""
    r = self.comR

```

```

n = len(self.chrom)
n2 = int(n//2)
i1 = r.randrange(n2)
i2 = r.randrange(n2, n+1)
m = self.chrom[:i1]+other.chrom[i1:i2]+self.chrom[i2:]
d = 0
for i in range(i1,i2):
    if self.chrom[i] == other.chrom[i]: d += 1
d = float(d)/(i2-i1)
if d > 0.5: d = ga.comFitmax*0.1*d
else:      d = 0.0
return self.__class__(ga, m, d)

def fitness(self, ga):
    """The fitness corrected according to big or small is better, and
corrected with deficiency."""
    if self.ftns is None:
        self.ftns = self.justFitness(ga)    # Either bigger or smaller is
better
        if not ga.comBiggerIsBetter: self.ftns = ga.comFitmax - self.ftns
        rep = self.ftns > ga.bestall.fitnessr(ga)
        self.ftns -= self.defic
        if rep: ga.bestall = copy.copy(self)
    return self.ftns

def justFitness(self, ga):
    """The fitness of the animal; the bigger the better."""
    raise AttributeError("Method justFitness() should be overridden.")

def fitnessr(self, ga):
    """The real fitness (i.e. plus deficiency)."""
    return self.fitness(ga)+self.defic

def detail(self, ga, fw):
    """Details about the distribution represented by the animal."""
    pass

thanThresholdx = 1e-10 # Threshold for coordinate difference; if less the
coordinates are the same
                    # This constant accomodates ThanCad too.

def thanNearx(xa, xb):
    "Checks if two coordinates (x or y) coincide taking numerical error into
account."
    d = fabs(xb-xa)
    v = (fabs(xa)+fabs(xb))*0.5
    if v < thanThresholdx: return d < thanThresholdx
    return d < v*thanThresholdx

```


pointcl

```
from math import fabs
import random
import prodiagrafes
import parametroi_kampilis
from geom import plinint, klisi, d_klisi, proarea, elegxos_s
import ery

class Point:
    """Computes random grade points, the elevation of the grade points
    and the area between grade and ground line."""
    ve, s_max, hk, hw = prodiagrafes.vasikes_parametroi()
    embmax = 1.0e100

    @classmethod
    def setGround(cls, xth, y):
        "Set the ground and number of nodes for all objects in this class."
        cls.xth = tuple(xth)
        cls.y = tuple(y)

    def __init__(self, a, xers=None, yers=None):
        "Set the geometry of the profile; compute random nodes if needed."
        self.a = a
        if xers is None:
            self.setRandomErs()
        else:
            assert len(xers) == a+2
            self.xers = list(xers)
            self.analyticYers()
        self.computeGeom()

    def computeGeom(self):
        "(Re)compute geometry of the profile."
        self.s = klisi(self.xers, self.yers)
        self.ds = d_klisi(self.xers, self.yers)
        self.h = parametroi_kampilis.dtrmn_h(Point.hw, Point.hk, self.s)
        self.t = parametroi_kampilis.dis_t(self.h, self.ds)
        self.embOverlapping = self.penaltyOverlapping()
#Additional area (penalty) due to overlapping
        self.embKlish = fabs(elegxos_s(self.xers, self.yers, Point.s_max))
#Additional area (penalty) due to excess slope
        self.embGeom = proarea(self.edafery()) #Area
of profile
        self.emb = self.embGeom + self.embOverlapping + self.embKlish
```

```

def setRandomErs(self):
    "(Re)set random nodes."
    xers = []
    xers.append(self.xth[0])
    xers.append(self.xth[-1])
    for i in range(self.a): # a is the number of grade points between the
first and last station
        xers.append(random.uniform(xers[0], xers[1]))
    xers.sort()
    self.xers = xers
    self.analyticYers()

def analyticYers(self):
    "Compute yers analytically."
    import numpy as np
    xth = np.array(self.xth)
    a, b, k = ery.exis(xth, np.array(self.y), self.xers[1:-1])
    self.yers = ery.ypolNodes(self.xers[1:-1], a, b)
    self.yers.insert(0, self.y[0])
    self.yers.append(self.y[-1])

def penaltyOverlapping(self):
    "Penalty due to overlapping of two consecutive vertical curves."
    penalty = 0.0
    for e in range(1, len(self.t)):
        tt = fabs(self.t[e]) + fabs(self.t[e-1])
        xx = self.xers[e] - self.xers[e-1]
        if tt > xx:
            penalty += (tt-xx)*30.0
    return penalty

def edafery(self):
    """Computes the grade line for all ground points and the ground line for
all grade points."""
    xeds2 = self.xth
    yeds2 = self.y
    xarx = xeds2[0]
    xtel = xeds2[-1]
    basic_x = parametroi_kampilis.curve(self.xers, self.ds, self.h) #Start
x and end x of all curves
    cc3 = [(b_x, plinint(xeds2, yeds2, b_x), plinint(self.xers, self.yers,
b_x)) for b_x in basic_x
            if xarx<b_x<xtel] #If we have overalapping, basic_x may be out
of the profile
    cc1 = [(xer, plinint(xeds2, yeds2, xer),
            parametroi_kampilis.in_out_curve(self.xers, self.yers, xer,
self.ds, self.h))
            for (xer, yer) in zip(self.xers, self.yers)]
    cc2 = [(xed, yed, parametroi_kampilis.in_out_curve(self.xers, self.yers,

```

```

xed, self.ds, self.h)) for (xed, yed) in zip(xeds2, yeds2)]
    cc2.extend(cc1)
    cc2.extend(cc3)
    cc2.sort()
    return cc2

```

ery

```

import bisect
import numpy as np
from numpy.linalg import lstsq, LinAlgError
from matplotlib import pyplot as pl

def ery(filnam):
    v = np.loadtxt(filnam)
    xth = v[:, 0]
    yed = v[:, 1]
    del v

    nu = 10
    dx = xth[-1]-10.0 - (xth[0] + 10.0)
    u = np.random.rand(nu) * dx + (xth[0] + 10.0)
    u.sort()
    a, b, k = exis(xth, yed, u)
    yer = ypoler(xth, a, b, k)
    pl.figure()
    pl.plot(xth, yed)
    #pl.hold(True)
    pl.plot(xth, yer, 'r')
    pl.savefig('q1.jpg')

```

```

def ypolNodes(u, a, b):
    "Compute the y of the fit line at the ndoes."
    yu = []
    for j in range(len(u)):
        yu.append(a[j] * u[j] + b[j])
    return yu

```

```

def ypoler(xth, a, b, k):
    "Compute grade line as the best line to fit the points."
    NN = len(xth)
    n = len(a)
    yer = np.zeros((NN,))
    jp = 0
    for j in range(n):
        if j < n-1: je = k[j]
        else:      je = NN;
        yer[jp:je] = a[j]*xth[jp:je] + b[j];
        jp = je

```

```

return yer

def exis(xth, yed, u):
    "find the equations of lines that best fit the points."
    n = len(u)
    NN = len(xth)
    assert n+2 <= NN, 'More unknowns than equations'
    k = np.zeros((n,), np.int)
    for j in range(n):
        k[j] = bisect.bisect(xth, u[j]) #this is 1 position to the right of the
value (xth)
    A = np.zeros((NN, n+2))
    A[:, 0] = 1.0;
    A[0:k[0], 1] = xth[0:k[0]]
    A[k[0]:, 1] = u[0]
    for j in range(3-1, n+1):
        A[k[j-2]:k[j-1], j] = xth[k[j-2]:k[j-1]] - u[j-2]
        A[k[j-1]:, j] = u[j-1] - u[j-2]
    A[k[n-1]:, n+2-1] = xth[k[n-1]:] - u[n-1]
    x, terr = lsmsolve(A, yed)
    if x is None: raise ValueError(terr)
    a = x[1:]
    b = np.zeros((n+1,))
    b[0] = x[0]
    for j in range(n):
        b[j+1] = a[j]*u[j]+b[j]-a[j+1]*u[j]
    return a, b, k

def lsmsolve(A, B):
    "Solve the Least square method problem defined by matrixes A and B."
    try:
        x, residual, rank, s = lstsq(A, B, rcond=-1.0)
    except LinAlgError as why:
        print(why)
        return None, why
    try: return x[:, 0], "" #2016_01_12thanasis:This converts shape from (333,
1) to (333,)
        #Otherwise x[1] is an array, not a scalar
    except: return x, "" #Thanasis2016_04_16: Changed again to normal???"

if __name__ == "__main__":
    ery("art1.mhk")

```

